# Package 'stops’ 

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Title Structure Optimized Proximity Scaling
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Description A collection of methods that fit nonlinear distance transformations in multidimensional scaling (MDS) and trade-off the fit with structure considerations to find optimal parameters also known as structure optimized proximity scaling (STOPS) (Rusch, Mair \& Hornik, 2023,[doi:10.1007/s11222-022-10197-w](doi:10.1007/s11222-022-10197-w)). The package contains various functions, wrappers, methods and classes for fitting, plotting and displaying different MDS models in a STOPS framework like Torgerson (classical) scaling, scaling by majorizing a complex function (SMACOF), Sammon mapping, elastic scaling, symmetric SMACOF, spherical SMACOF, s-stress, r-stress, power MDS, power elastic scaling, power Sammon mapping, power stress MDS (POST-MDS), approximate power stress, BoxCox MDS, local MDS and Isomap. All of these models can also be fit individually with given hyperparameters or by optimizing over hyperparameters based on fit only (i.e., no structure considerations). The package further contains functions for optimization, specifically the adaptive Luus-Jaakola algorithm and a wrapper for Bayesian optimization with treed Gaussian process with jumps to linear models, and functions for various c-structuredness indices.

Depends R (>= 3.5.0), smacof, rgl
Imports cordillera, MASS, pso, scatterplot3d, acepack, minerva,
energy, DiceOptim, DiceKriging, tgp, pomp, vegan, scagnostics,
clue, cmaes, dfoptim, nloptr
Enhances stats
Suggests sp, R.rsp
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$R$ topics documented:
apStressMin ..... 4
BankingCrisesDistances ..... 5
bcStressMin ..... 6
cmds ..... 8
cmdscale ..... 8
coef.stops ..... 9
conf_adjust ..... 9
c association ..... 10
c_clumpiness ..... 11
c_clusteredness ..... 11
c_complexity ..... 13
c_convexity ..... 14
c_dependence ..... 14
c_faithfulness ..... 15
c_functionality ..... 16
c_hierarchy ..... 17
c_inequality ..... 17
c_linearity ..... 18
c_manifoldness ..... 19
c_mine ..... 20
c_nonmonotonicity ..... 20
c_outlying ..... 21
c_regularity ..... 22
c_skinniness ..... 23
c_sparsity ..... 24
c_striatedness ..... 24
c_stringiness ..... 25
doubleCenter ..... 26
enorm ..... 26
knn_dist ..... 27
ljoptim ..... 27
lmds ..... 29
mkBmat ..... 30
mkPower ..... 31
mkPower2 ..... 31
Pendigits500 ..... 32
plot.cmdscaleE ..... 32
plot.smacofP ..... 34
plot.stops ..... 36
plot3d.cmdscaleE ..... 37
plot3d.stops ..... 38
plot3dstatic ..... 38
plot3dstatic.cmdscaleE ..... 39
plot3dstatic.stops ..... 40
powerStressMin ..... 40
print.cmdscale ..... 42
print.sammon ..... 43
print.stops ..... 43
print.summary.smacofP ..... 44
print.summary.stops ..... 44
procruster ..... 45
residuals.stops ..... 45
sammon ..... 46
secularEq ..... 46
sqdist ..... 47
stoploss ..... 47
stops ..... 48
stop_apstress ..... 54
stop_bcstress ..... 55
stop_cmdscale ..... 57
stop_elastic ..... 58
stop_isomap1 ..... 59
stop_isomap2 ..... 61
stop_lmds ..... 63
stop_powerelastic ..... 64
stop_powermds ..... 65
stop_powersammon ..... 67
stop_powerstress ..... 68
stop_rpowerstress ..... 70
stop_rstress ..... 71
stop_sammon ..... 73
stop_sammon2 ..... 74
stop_smacofSphere ..... 75
stop_smacofSym ..... 77
stop_sstress ..... 78
summary.cmdscale ..... 80
summary.sammon ..... 80
summary.smacofP ..... 81
summary.stops ..... 81
Swissroll ..... 82
tgpoptim ..... 82
torgerson ..... 84
Index ..... 85

```
apStressMin
```

Approximate Power Stress SMACOF

## Description

Minimize approximate power stress by minimization-majorization.

## Usage

apStressMin( delta, tau $=1$, ups = 1,
weightmat = 1 - diag(nrow(delta)),
init = NULL,
ndim $=2$,
eps $=1 \mathrm{e}-06$,
itmax = 1000,
verbose = FALSE
)

## Arguments

| delta | dist object or a symmetric, numeric data.frame or matrix of distances |
| :--- | :--- |
| tau | the power of the transformation of the proximities; defaults to 1 |
| ups | the power of the transformation for weightmat; defaults to 1 |
| weightmat | a square, symmetric matrix of finite weights (same dimensions as delta) |
| init | starting configuration |
| ndim | dimension of the configuration; defaults to 2 |
| eps | numeric accuracy of the iteration |
| itmax | maximum number of iterations |
| verbose | should iteration output be printed; if TRUE then yes |

## Value

an object of class 'smacofP' (inheriting from 'smacofB', see smacofSym). It is a list with the components

- delta: Observed dissimilarities, not normalized
- obsdiss: Observed transformed dissimilarities
- dhats: Observed transformed dissimilarities, normalized
- confdist: Configuration dissimilarities, NOT normalized
- conf: Matrix of fitted configuration, NOT normalized
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point (based on stress.en)
- ndim: Number of dimensions
- model: Name of MDS model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix
- pars: hyperparameter vector theta
and some additional components
- stress.m: default stress for the COPS and STOP defaults to the explicitly normalized stress on the normalized, transformed dissimilarities. The square of stress-1 in stress.
- deltaorig: observed, untransformed dissimilarities
- tau: tau parameter
- ups: upsilon parameter


## Author(s)

Thomas Rusch

## See Also

```
smacofSym
```


## Examples

```
dis<-smacof::kinshipdelta
res<-apStressMin(as.matrix(dis),tau=2,ups=0.7)
res
summary(res)
plot(res)
```

BankingCrisesDistances

Banking Crises Distances

## Description

Matrix of Jaccard distances between 70 countries (Hungary and Greece were combined to be the same observation) based on their binary time series of having had a banking crises in a year from 1800 to 2010 or not. See data(bankingCrises) in package Ecdat for more info. The last column is Reinhart \& Rogoffs classification as a low (3), middle- (2) or high-income country (1).

## Format

A $69 \times 70$ matrix.

## Source

data(bankingCrises) in library(Ecdat)
bcStressMin An MDS version for minimizing BoxCox Stress (Chen \& Buja 2013)

## Description

An MDS version for minimizing BoxCox Stress (Chen \& Buja 2013)

## Usage

```
    bcStressMin(
        delta,
        init = NULL,
        verbose = 0,
        ndim = 2,
        mu = 1,
        lambda = 1,
        rho = 0,
        itmax = 2000,
        addD0 = 1e-04
    )
```


## Arguments

delta dissimilarity or distance matrix
init initial configuration. If NULL a classical scaling solution is used.
verbose prints progress if $>3$.
ndim the dimension of the configuration
mu mu parameter. Should be 0 or larger for everything working ok. If mu<0 it works but the model is strange and normalized stress tends towards 0 regardless of fit. Use normalized stress at your own risk in that case.
lambda lambda parameter. Must be larger than 0.
rho the rho parameter.
itmax number of optimizing iterations, defaults to 2000.
addD0 a small number that's added for $\mathrm{D}(\mathrm{X})=0$ for numerical evaluation of worst fit (numerical reasons, see details). If addD0 $=0$ the normalized stress for mu! $=0$ and mu+lambda! $=0$ is correct, but will give useless normalized stress for mu=0 or mu+lambda! $=0$.

## Details

For numerical reasons with certain parameter combinations, the normalized stress uses a configuration as worst result where every $\mathrm{d}(\mathrm{X})$ is $0+$ addD0. The same number is not added to the delta so there is a small inaccuracy of the normalized stress (but negligible if min(delta)»addD0). Also, for $m u<0$ or mu+lambda<0 the normalization cannot generally be trusted (in the worst case of $D(X)=0$ one would have an $\left.0^{\wedge}(-a)\right)$.

## Value

an object of class 'bemds' (also inherits from 'smacofP'). It is a list with the components

- delta: Observed dissimilarities, not normalized
- obsdiss: Observed transformed dissimilarities, not normalized
- confdist: Configuration dissimilarities, NOT normalized
- conf: Matrix of fitted configuration, NOT normalized
- stress: Default stress (stress 1 ; sqrt of explicitly normalized stress)
- ndim: Number of dimensions
- model: Name of MDS model
- niter: Number of iterations
- nobj: Number of objects
- pars: hyperparameter vector theta
and some additional components
- stress.m: default stress is the explicitly normalized stress on the normalized, transformed dissimilarities
- deltaorig: observed, untransformed dissimilarities
- mu: mu parameter (for attraction)
- lambda: lambda parameter (for repulsion)
- rho: rho parameter (for weights)

Author(s)
Lisha Chen \& Thomas Rusch

## Examples

```
dis<-smacof::kinshipdelta
res<-bcStressMin(as.matrix(dis),mu=2,lambda=1.5,rho=0)
res
summary(res)
plot(res)
```


## Description

normalization function Classical Scaling

## Usage

cmds(Do)

## Arguments

$$
\text { Do } \quad \text { dissimilarity matrix }
$$

cmdscale Wrapper to cmdscale for S3 class

## Description

Wrapper to cmdscale for S3 class

## Usage

cmdscale(d, k = 2, eig = TRUE, ...)

## Arguments

d
a distance structure such as that returned by 'dist' or a full symmetric matrix containing the dissimilarities
$\mathrm{k} \quad$ the maximum dimension of the space which the data are to be represented in
eig indicates whether eigenvalues should be returned.
... additional parameters passed to cmdscale. See cmdscale

## Details

overloads base::cmdscale and adds class attributes for which there are methods. The functionality is duplicated in the cops package.

## Value

An object of class 'cmdscaleE' and inheriting from cmdscale. This function just adds an extra slot to the list with the call, adds column labels to the \$points.

```
coef.stops S3 coef method for stops objects
```


## Description

S3 coef method for stops objects

## Usage

\#\# S3 method for class 'stops'
coef(object, ...)

## Arguments

| object | object of class stops |
| :--- | :--- |
| $\ldots$ | addditional arguments |

## Value

a vector of hyperparmeters theta
conf_adjust conf_adjust: a function to procrustes adjust two matrices

## Description

conf_adjust: a function to procrustes adjust two matrices

## Usage

conf_adjust (conf1, conf2, verbose = FALSE, eps = 1e-12, itmax = 100)

## Arguments

| conf1 | reference configuration, a numeric matrix |
| :--- | :--- |
| conf2 | another configuration to be adjusted, a numeric matrix |
| verbose | should adjustment be output; default to FALSE |
| eps | numerical accuracy |
| itmax | maximum number of iterations |

## Value

A list of configuration matrices. The 'ref.conf' is the reference configuration, the 'other.conf' is the Procrustes adjusted configuration and the 'comparison.conf' is the one that was adjusted.
c-association calculates the c-association based on the maximal information coefficient We define c-association as the aggregated association between any two columns in confs

## Description

c-association calculates the c-association based on the maximal information coefficient We define c-association as the aggregated association between any two columns in confs

## Usage

c_association(
confs,
aggr $=\max$,
alpha $=0.6$,
$C=15$,
var.thr $=1 \mathrm{e}-05$,
zeta $=$ NULL
)

## Arguments

| confs | a numeric matrix or data frame |
| :--- | :--- |
| aggr |  |
| the aggregation function for configurations of more than two dimensions. De- |  |
| faults to max. |  |
| an optional number of cells allowed in the X-by-Y search-grid. Default value is |  |
| 0.6 |  |$\quad$| an optional number determining the starting point of the X-by-Y search-grid. |
| :--- |
| C |
| Vhen trying to partition the x-axis into X columns, the algorithm will start with |
| at most C X clumps. Default value is 15. |

Value
a numeric value; association (aggregated maximal information coefficient MIC, see mine)

## Examples

```
x<-seq(-3,3,length.out=200)
y<-sqrt(3^2-x^2)
z<- sin(y-x)
```

```
confs<-cbind(x,y,z)
```

c_association(confs)

```
c_clumpiness c-clumpiness
```


## Description

Measures the c-clumpiness structure

## Usage

c_clumpiness(conf, aggr = max)

## Arguments

conf A numeric matrix.
aggr the aggregation function for configurations of more than two dimensions. Defaults to max.

## Value

a numeric value; clumpiness (see scagnostics)

## Examples

```
    delts<-smacof::kinshipdelta
    conf<-smacof::smacofSym(delts)$conf
    plot(conf,pch=19,asp=1)
    c_clumpiness(conf)
```

    c_clusteredness c-clusteredness calculates c-clusteredness as the OPTICS cordillera.
                        The higher the more clustered.
    
## Description

c-clusteredness calculates c-clusteredness as the OPTICS cordillera. The higher the more clustered.

```
Usage
    c_clusteredness(
        confs,
        minpts = 2,
        q = 2,
    epsilon = 2 * max(dist(confs)),
    distmeth = "euclidean",
    dmax = NULL,
    digits = 10,
    scale = 0,
    )
```


## Arguments

| confs | a numeric matrix or a dist object |
| :---: | :---: |
| minpts | The minimum number of points that must make up a cluster in OPTICS (corresponds to k in the paper). It is passed to optics where it is called minPts. Defaults to 2. |
| q | The norm used for the Cordillera. Defaults to 2. |
| epsilon | The epsilon parameter for OPTICS (called epsilon_max in the paper). Defaults to 2 times the maximum distance between any two points. |
| distmeth | The distance to be computed if X is not a symmetric matrix or a dist object (otherwise ignored). Defaults to Euclidean distance. |
| dmax | The winsorization value for the highest allowed reachability. If used for comparisons between different configurations this should be supplied. If no value is supplied, it is NULL (default); then dmax is taken from the data as the either epsilon or the largest reachability, whatever is smaller. |
| digits | The precision to round the raw Cordillera and the norm factor. Defaults to 10. |
| scale | Should $X$ be scaled if it is an asymmetric matrix or data frame? Can take values TRUE or FALSE or a numeric value. If TRUE or 1 , standardisation is to mean=0 and $\mathrm{sd}=1$. If 2, no centering is applied and scaling of each column is done with the root mean square of each column. If 3, no centering is applied and scaling of all columns is done as $\mathrm{X} / \max$ (standard deviation(allcolumns)). If 4, no centering is applied and scaling of all columns is done as $\mathrm{X} / \max (\mathrm{rmsq}($ allcolumns)). If FALSE, 0 or any other numeric value, no standardisation is applied. Defaults to 0 . |
|  | Additional arguments to be passed to cordillera: :cordillera |

## Value

a numeric value; clusteredness (see cordillera)

## Examples

delts<-smacof::kinshipdelta
dis<-smacofSym(delts)\$confdist
c_clusteredness(dis,minpts=3)
c_complexity c-complexity Calculates the c-complexity based on the minimum cell number We define c-complexity as the aggregated minimum cell number between any two columns in confs This is one of few cstructuredness indices not between 0 and 1 , but can be between 0 and (theoretically) infinity

## Description

c-complexity Calculates the c-complexity based on the minimum cell number We define c-complexity as the aggregated minimum cell number between any two columns in confs This is one of few cstructuredness indices not between 0 and 1 , but can be between 0 and (theoretically) infinity

## Usage

```
    c_complexity(
        confs,
        aggr = min,
        alpha = 1,
        C = 15,
        var.thr = 1e-05,
        zeta = NULL
    )
```


## Arguments

| confs | a numeric matrix or data frame <br> aggr <br> the aggregation function for configurations of more than two dimensions. De- <br> faults to min. <br> alpha |
| :--- | :--- |
| an optional number of cells allowed in the X-by-Y search-grid. Default value is |  |
| C | an optional number determining the starting point of the X-by-Y search-grid. <br> When trying to partition the x-axis into X columns, the algorithm will start with <br> at most C X clumps. Default value is 15. |
| var.thr | minimum value allowed for the variance of the input variables, since mine can <br> not be computed in case of variance close to 0. Default value is 1e-5. <br> integer in [0,1] (?). If NULL (default) it is set to 1-MIC. It can be set to zero for <br> noiseless functions, but the default choice is the most appropriate parametriza- <br> tion for general cases (as stated in Reshef et al.). It provides robustness. |

## Value

a numeric value; complexity (aggregated minimum cell number MCN, see mine)

## Examples

```
    x<-seq(-3,3, length.out=200)
    y<-sqrt(3^2-x^2)
    z<- sin(y-x)
    confs<-cbind(x,y,z)
    c_complexity(confs)
```

    c_convexity c-convexity
    
## Description

Measures the c-convexity structure

## Usage

c_convexity (conf, aggr = max)

## Arguments

$$
\text { conf } \quad \text { A numeric matrix. }
$$

aggr the aggregation function for configurations of more than two dimensions. Defaults to max.

## Value

a numeric value; convexity (see scagnostics)

## Examples

```
    delts<-smacof::kinshipdelta
    conf<-smacof::smacofSym(delts)$conf
    plot(conf,pch=19,asp=1)
    c_convexity(conf)
```

    c_dependence c-dependence calculates c-dependence as the aggregated distance
        correlation of each pair if nonidentical columns
    
## Description

c-dependence calculates c-dependence as the aggregated distance correlation of each pair if nonidentical columns

## Usage

c_dependence (confs, aggr = max, index = 1)

## Arguments

confs
a numeric matrix or data frame
aggr the aggregation function for configurations of more than two dimensions. Defaults to max.
index exponent on Euclidean distance, in $(0,2]$

## Value

a numeric value; dependence (aggregated distance correlation)

## Examples

```
x<-1:10
y<-2+3*x+rnorm(10)
confs<-cbind(x,y)
c_dependence(confs,1.5)
```

c_faithfulness c-faithfulness calculates the c-faithfulness based on the index by Chen
and Buja 2013 (M_adj) with equal input neigbourhoods

## Description

c-faithfulness calculates the c-faithfulness based on the index by Chen and Buja 2013 (M_adj) with equal input neigbourhoods

## Usage

c_faithfulness(confs, obsdiss, k = 3, ...)

## Arguments

| confs | a numeric matrix or a dist object |
| :--- | :--- |
| obsdiss | a symmetric numeric matrix or a dist object |
| k | the number of nearest neighbours to be looked at |
| $\ldots$ | additional arguments passed to dist() |

## Value

a numeric value; faithfulness

## Examples

$$
\begin{aligned}
& \text { delts<-smacof::kinshipdelta } \\
& \text { dis<-smacofSym(delts)\$confdist } \\
& \text { c_faithfulness(dis,delts,k=3) }
\end{aligned}
$$

c_functionality $c$-functionality calculates the c-functionality based on the maximum edge value We define c-functionality as the aggregated functionality between any two columns of confs

## Description

c-functionality calculates the c-functionality based on the maximum edge value We define c-functionality as the aggregated functionality between any two columns of confs

## Usage

c_functionality(
confs,
aggr $=$ max, alpha = 1, $C=15$, var.thr $=1 \mathrm{e}-05$, zeta $=$ NULL
)

## Arguments

$$
\begin{array}{ll}
\text { confs } & \begin{array}{l}
\text { a numeric matrix or data frame } \\
\text { aggr } \\
\text { the aggregation function for configurations of more than two dimensions. De- } \\
\text { faults to mean }
\end{array} \\
\text { alpha } & \begin{array}{l}
\text { an optional number of cells allowed in the X-by-Y search-grid. Default value is } \\
1
\end{array} \\
\text { C } & \begin{array}{l}
\text { an optional number determining the starting point of the X-by-Y search-grid. } \\
\text { When trying to partition the x-axis into X columns, the algorithm will start with } \\
\text { at most C X clumps. Default value is } 15 .
\end{array} \\
\text { var. thr } & \begin{array}{l}
\text { minimum value allowed for the variance of the input variables, since mine can } \\
\text { not be computed in case of variance close to } 0 \text {. Default value is 1e-5. } \\
\text { integer in [0,1] (?). If NULL (default) it is set to 1-MIC. It can be set to zero for } \\
\text { noiseless functions, but the default choice is the most appropriate parametriza- } \\
\text { tion for general cases (as stated in Reshef et al.). It provides robustness. }
\end{array}
\end{array}
$$

## Value

a numeric value; functionality (aggregated maximaum edge value MEV, see mine)

## Examples

```
x<-seq(-3,3,length.out=200)
y<-sqrt(3^2-x^2)
z<- sin(y-x)
```

```
confs<-cbind(x,y,z)
```

c_functionality(confs)
c_hierarchy c-hierarchy captures how well a partition/ultrametric (obtained by hclust) explains the configuration distances. Uses variance explained for euclidean distances and deviance explained for everything else.

## Description

c-hierarchy captures how well a partition/ultrametric (obtained by hclust) explains the configuration distances. Uses variance explained for euclidean distances and deviance explained for everything else.

## Usage

c_hierarchy(confs, $\mathrm{p}=2$, agglmethod = "complete")

## Arguments

$$
\begin{array}{ll}
\text { confs } & \text { a numeric matrix } \\
\mathrm{p} & \text { the parameter of the Minokwski distances ( } \mathrm{p}=2 \text { euclidean and } \mathrm{p}=1 \text { is manhattan) } \\
\text { agglmethod } & \text { the method used for creating the clustering, see hclust. }
\end{array}
$$

Value
a numeric value; hierarchy (see cl_validity)

## Examples

```
delts<-smacof::kinshipdelta
conf<-smacofSym(delts)$conf
c_hierarchy(conf,p=2,agglmethod="single")
```

c_inequality
c-inequality Calculates c-inequality (as in an economic measure of inequality) as Pearsons coefficient of variation of the fitted distance matrix. This can help with avoiding degenerate solutions. This is one of few c-structuredness indices not between 0 and 1, but 0 and infinity.

## Description

c-inequality Calculates c-inequality (as in an economic measure of inequality) as Pearsons coefficient of variation of the fitted distance matrix. This can help with avoiding degenerate solutions. This is one of few c -structuredness indices not between 0 and 1 , but 0 and infinity.

## Usage

c_inequality(confs)

## Arguments

$$
\text { confs } \quad \text { a numeric matrix or data frame }
$$

## Value

a numeric value; inequality (Pearsons coefficient of variation of the fitted distance matrix)

## Examples

$x<-1: 10$
$y<-2+3 * x+r n o r m(10)$
$z<-\sin (y-x)$
confs<-cbind $(z, y, x)$
c_inequality(confs)
c_linearity c-linearity calculates c-linearity as the aggregated multiple correlation of all columns of the configuration.

## Description

c-linearity calculates c-linearity as the aggregated multiple correlation of all columns of the configuration.

## Usage

c_linearity (confs, aggr = max)

## Arguments

$\begin{array}{ll}\text { confs } & \text { a numeric matrix or data frame } \\ \text { aggr } & \text { the aggregation function for configurations of more than two dimensions. De- } \\ \text { faults to max. }\end{array}$

## Value

a numeric value; linearity (aggregated multiple correlation of all columns of the configuration)

## Examples

```
x<-1:10
y<-2+3*x+rnorm(10)
z<- sin(y-x)
confs<-cbind(z,y,x)
c_linearity(confs)
```

$$
\begin{array}{ll}
\text { c_manifoldness } & \text { c-manifoldness calculates c-manifoldness as the aggregated max- } \\
\text { imal correlation coefficient (i.e., Pearson correlation of the ACE } \\
\text { transformed variables) of all pairwise combinations of two different } \\
\text { columns in confs. If there is an NA (happens usually when the optimal } \\
\text { transformation of any variable is a constant and therefore the covari- } \\
\text { ance is } 0 \text { but also one of the sds in the denominator), it gets skipped. }
\end{array}
$$

## Description

c-manifoldness calculates c-manifoldness as the aggregated maximal correlation coefficient (i.e., Pearson correlation of the ACE transformed variables) of all pairwise combinations of two different columns in confs. If there is an NA (happens usually when the optimal transformation of any variable is a constant and therefore the covariance is 0 but also one of the sds in the denominator), it gets skipped.

## Usage

c_manifoldness(confs, aggr = max)

## Arguments

| confs | a numeric matrix or data frame |
| :--- | :--- |
| aggr | the aggregation function for configurations of more than two dimensions. De- |
| faults to max. |  |

Value
a numeric value; manifoldness (aggregated maximal correlation, correlation of ACE tranformed $x$ and $y$, see ace)

## Examples

```
\(x<--100: 100\)
\(y<-s q r t\left(100^{\wedge} 2-x^{\wedge} 2\right)\)
confs<-cbind( \(x, y\) )
c_manifoldness(confs)
```


## Description

wrapper for getting the mine coefficients

## Usage

c_mine (confs, master $=$ NULL, alpha $=0.6, \mathrm{C}=15$, var.thr $=1 \mathrm{e}-05$, zeta $=$ NULL)

## Arguments

confs a numeric matrix or data frame with two columns
master the master column
alpha an optional number of cells allowed in the X-by-Y search-grid. Default value is 0.6

C an optional number determining the starting point of the X -by-Y search-grid. When trying to partition the x -axis into X columns, the algorithm will start with at most C X clumps. Default value is 15 .
var.thr minimum value allowed for the variance of the input variables, since mine can not be computed in case of variance close to 0 . Default value is $1 \mathrm{e}-5$.
zeta integer in [0,1] (?). If NULL (default) it is set to 1-MIC. It can be set to zero for noiseless functions, but the default choice is the most appropriate parametrization for general cases (as stated in Reshef et al. SOM; they call it epsilon in the paper). It provides robustness.
c_nonmonotonicity c-nonmonotonicity calculates the c-nonmonotonicity based on the maximum asymmetric score We define c-nonmonotonicity as the aggregated nonmonotonicity between any two columns in confs this is one of few c-structuredness indices not between 0 and 1

## Description

c-nonmonotonicity calculates the c-nonmonotonicity based on the maximum asymmetric score We define c-nonmonotonicity as the aggregated nonmonotonicity between any two columns in confs this is one of few $c$-structuredness indices not between 0 and 1

## Usage

```
    c_nonmonotonicity(
        confs,
        aggr = max,
        alpha = 1,
        C = 15,
        var.thr = 1e-05,
        zeta = NULL
    )
```


## Arguments

confs
aggr the aggregation function for configurations of more than two dimensions. Defaults to max.
alpha an optional number of cells allowed in the X-by-Y search-grid. Default value is 1

C an optional number determining the starting point of the X -by-Y search-grid. When trying to partition the x -axis into X columns, the algorithm will start with at most C X clumps. Default value is 15 .
var.thr minimum value allowed for the variance of the input variables, since mine can not be computed in case of variance close to 0 . Default value is $1 \mathrm{e}-5$.
zeta integer in [0,1] (?). If NULL (default) it is set to 1-MIC. It can be set to zero for noiseless functions, but the default choice is the most appropriate parametrization for general cases (as stated in Reshef et al. SOM). It provides robustness.

## Value

a numeric value; nonmonotonicity (aggregated maximal asymmetric score MAS, see mine)

## Examples

```
x<-seq(-3,3,length.out=200)
y<-sqrt(3^2-x^2)
z<- sin(y-x)
confs<-cbind(x,y,z)
c_nonmonotonicity(confs)
```

```
c_outlying c-outlying
```


## Description

Measures the c-outlying structure

## Usage

c_outlying(conf, aggr = max)

## Arguments

| conf | A numeric matrix. |
| :--- | :--- |
| aggr | the aggregation function for configurations of more than two dimensions. De- |
| faults to max. |  |

## Value

a numeric value; outlying (see scagnostics)

## Examples

```
delts<-smacof::kinshipdelta
conf3<-smacof::smacofSym(delts,ndim=3)$conf
c_outlying(conf3)
```

```
c_regularity c-regularity calculates c-regularity as l-OPTICS cordillera for k=2.
```

    The higher the more regular.
    
## Description

c-regularity calculates c-regularity as 1 - OPTICS cordillera for $\mathrm{k}=2$. The higher the more regular.

## Usage

c_regularity(
confs,
$q=1$,
epsilon $=2$ * max(dist(confs)),
distmeth = "euclidean",
dmax = NULL,
digits = 10,
scale $=0$,
...
)

## Arguments

confs a numeric matrix or a dist object
$\mathrm{q} \quad$ The norm used for the Cordillera. Defaults to 1 (and should always be 1 imo ).
epsilon The epsilon parameter for OPTICS (called epsilon_max in the paper). Defaults to 2 times the maximum distance between any two points.

| distmeth | The distance to be computed if X is not a symmetric matrix or a dist object (otherwise ignored). Defaults to Euclidean distance. |
| :---: | :---: |
| dmax | The winsorization value for the highest allowed reachability. If used for comparisons this should be supplied. If no value is supplied, it is NULL (default), then dmax is taken from the data as minimum of epsilon or the largest reachability. |
| digits | The precision to round the raw Cordillera and the norm factor. Defaults to 10 . |
| scale | Should $X$ be scaled if it is an asymmetric matrix or data frame? Can take values TRUE or FALSE or a numeric value. If TRUE or 1 , standardisation is to mean $=0$ and $\mathrm{sd}=1$. If 2 , no centering is applied and scaling of each column is done with the root mean square of each column. If 3 , no centering is applied and scaling of all columns is done as $\mathrm{X} / \max$ (standard deviation(allcolumns)). If 4 , no centering is applied and scaling of all columns is done as $\mathrm{X} / \max (\mathrm{rmsq}($ allcolumns $)$ ). If FALSE, 0 or any other numeric value, no standardisation is applied. Defaults to 0. |
|  | Additional arguments to be passed to cordillera |

## Value

a numeric value; regularity

## Examples

```
hpts<-expand.grid(seq(-5,5),seq(-5,5))
```

c_regularity(hpts)
hpts2<-cbind(jitter(hpts[,1]), jitter(hpts[,2]))
c_regularity(hpts2)

```
c_skinniness c-skinniness
```


## Description

Measures the c-skinniness structure

## Usage

c_skinniness(conf, aggr = max)

## Arguments

$$
\begin{array}{ll}
\text { conf } & \text { A numeric matrix. } \\
\text { aggr } & \text { the aggregation function for configurations of more than two dimensions. De- } \\
\text { faults to max. }
\end{array}
$$

## Value

a numeric value; skininess (see scagnostics)

## Examples

delts<-smacof::kinshipdelta
conf<-smacof: : smacofSym(delts) \$conf
plot (conf, pch=19, asp=1)
c_skinniness(conf)

```
    c_sparsity c-sparsity
```


## Description

Measures the c-sparsity structure

## Usage

c_sparsity(conf, aggr = max)

## Arguments

conf
A numeric matrix.
aggr
the aggregation function for configurations of more than two dimensions. Defaults to max.

## Value

a numeric value; sparsity (see scagnostics)

## Examples

```
delts<-smacof::kinshipdelta
    conf<-smacof::smacofSym(delts)$conf
    plot(conf,pch=19,asp=1)
    c_sparsity(conf)
```

    C_striatedness c-striatedness
    
## Description

Measures the c-striatedness structure

## Usage

c_striatedness(conf, aggr = max)

## Arguments

conf
A numeric matrix.
aggr the aggregation function for configurations of more than two dimensions. Defaults to max.

## Value

a numeric value; striatedness (see scagnostics)

## Examples

```
delts<-smacof::kinshipdelta
conf<-smacof::smacofSym(delts)$conf
plot(conf,pch=19,asp=1)
c_striatedness(conf)
```

    c_stringiness c-stringiness
    
## Description

Measures the c-stringiness structure

## Usage

c_stringiness(conf, aggr = max)

## Arguments

conf
A numeric matrix.
aggr the aggregation function for configurations of more than two dimensions. Defaults to max.

## Value

a numeric value; stringiness (see scagnostics)

## Examples

```
delts<-smacof::kinshipdelta
conf<-smacof::smacofSym(delts)$conf
plot(conf,pch=19,asp=1)
c_stringiness(conf)
```

| doubleCenter $\quad$ double centering |
| :--- |

## Description

double centering

## Usage

doubleCenter (x)

## Arguments

x
numeric matrix

## Description

## Explicit Norm

## Usage

$\operatorname{enorm}(x, w=1)$

## Arguments

x
w numeric matrix
weight

## Value

a numeric scalar; the $\operatorname{sum}\left(w^{*} \mathrm{x}^{\wedge} 2\right)$
knn_dist calculate $k$ nearest neighbours from a distance matrix

## Description

calculate k nearest neighbours from a distance matrix

## Usage

knn_dist(dis, k)

## Arguments

dis distance matrix
$k \quad$ number of nearest neighbours (Note that with a tie, the function returns the alphanumerically first one!)
ljoptim (Adaptive) Version of Luus-Jaakola Optimization

## Description

Adaptive means that the search space reduction factors in the number of iterations; makes convergence faster at about 100 iterations

## Usage

ljoptim(
x,
fun,
...,
red $=$ ifelse(adaptive, 0.99, 0.95),
lower,
upper,
acc $=1 \mathrm{e}-06$,
accd $=1 \mathrm{e}-04$,
itmax = 1000,
verbose = 0,
adaptive = TRUE
)

## Arguments

| x | optional starting values |
| :---: | :---: |
| fun | function to minimize |
|  | additional arguments to be passed to the function to be optimized |
| red | value of the reduction of the search region |
| lower | The lower contraints of the search region |
| upper | The upper contraints of the search region |
| acc | if the numerical accuracy of two successive target function values is below this, stop the optimization; defaults to $1 \mathrm{e}-6$ |
| accd | if the width of the search space is below this, stop the optimization; defaults to 1e-4 |
| itmax | maximum number of iterations |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| adaptive | should the adaptive version be used? defaults to TRUE. |

## Value

A list with the components (optim)

- par The position of the optimimum in the search space (parameters that minimize the function; argmin fun)
- value The value of the objective function at the optimum (min fun)
- counts The number of iterations performed at convergence with entries fnction for the number of iterations and gradient which is always NA at the moment
- convergence 0 successful completion by the accd or acc criterion, 1 indicate iteration limit was reached, 99 is a problem
- message is NULL (only for compatibility or future use)


## Examples

```
fbana <- function(x) {
x1 <- x[1]
x2<- x[2]
100 * (x2 - x1 * x1)^2 + (1 - x1)^2
}
res1<-ljoptim(c(-1.2,1),fbana,lower=-5,upper=5, accd=1e-16,acc=1e-16)
res1
set.seed(210485)
fwild <- function (x) 10*sin(0.3*x)*sin(1.3*x^2) + 0.00001*x^4 + 0.2*x+80
plot(fwild, -50, 50, n = 1000, main = "ljoptim() minimising 'wild function'")
res2<-ljoptim(50, fwild,lower=-50,upper=50,adaptive=FALSE,accd=1e-16,acc=1e-16)
points(res2$par,res2$value,col="red",pch=19)
res2
```


## Description

An function for local MDS (Chen \& Buja 2006)

## Usage

lmds(delta, init $=$ NULL, $\operatorname{ndim}=3, k=2$, tau $=1$, itmax $=5000$, verbose $=0$ )

## Arguments

delta dissimilarity or distance matrix
init initial configuration. If NULL a classical scaling solution is used.
ndim the dimension of the configuration
$k \quad$ the k neighbourhood parameter
tau the penalty parameter (suggested to be in [0,1])
itmax number of optimizing iterations, defaults to 5000.
verbose $\quad$ prints progress if $>4$.

## Details

Note that k and tau are not independent. It is possible for normalized stress to become negative if the tau and k combination is so that the absolute repulsion for the found configuration dominates the local stress substantially less than the repulsion term does for the solution of $\mathrm{D}(\mathrm{X})=\mathrm{Delta}$, so that the local stress difference between the found solution and perfect solution is nullified. This can typically be avoided if tau is between 0 and 1 . If not, set k and or tau to a smaller value.

## Value

an object of class 'lmds' (also inherits from 'smacofP'). See powerStressMin. It is a list with the components as in power stress

- delta: Observed dissimilarities, not normalized
- obsdiss: Observed transformed dissimilarities, not normalized
- confdist: Configuration dissimilarities, NOT normalized
- conf: Matrix of fitted configuration, NOT normalized
- stress: Default stress (stress 1 ; sqrt of explicitly normalized stress)
- ndim: Number of dimensions
- model: Name of MDS model
- niter: Number of iterations
- nobj: Number of objects
- pars: hyperparameter vector theta
and some additional components
- stress.m: default stress is the explicitly normalized stress on the normalized, transformed dissimilarities
- deltaorig: observed, untransformed dissimilarities
- tau: tau parameter
- k: k parameter


## Author(s)

Lisha Chen \& Thomas Rusch

## Examples

```
dis<-smacof::kinshipdelta
res<- lmds(as.matrix(dis),k=2,tau=0.1)
res
summary(res)
plot(res)
```

mkBmat

## Description

MkBmat function (internal)

## Usage

mkBmat ( x )

## Arguments

x
matrix
mkPower MakePower Old

## Description

MakePower Old

## Usage

mkPower ( $\mathrm{x}, \mathrm{r}$ )

## Arguments

x
matrix
$r$
numeric (power)

## Value

the matrix to a power

| mkPower2 $\quad$ MakePower |
| :--- | :--- |

## Description

MakePower

## Usage

mkPower2(x, theta)

## Arguments

| $x$ | matrix |
| :--- | :--- |
| theta | numeric (power) |

```
Pendigits500 Pen digits
```


## Description

These data are a random sample of 500 of the 10992 pendigits data from Alimoglu (1996). The original data were from 44 writers who handwrote 250 times the digits $0, \ldots, 9$. The digits were written inside a rectangular box with a resolution of $500 \times 500$ pixels and the first 10 per writer were ignored for further analysis. This led to 10992 digits. They were recorded in small time intervals by following the trajectory of the pen on the $500 \times 500$ grid and then normalized. From the normalized trajectory 8 points ( $x$ and $y$ axis position) were randomly selected for each handwritten digit, leading to 16 predictors variables. We extarcted a random sample of 500 of them.

## Usage <br> data(Pendigits500)

## Format

A data frame with 500 rows and 17 variables

## Details

The variables are

- The rownames of Pendigits500 refer to the data point of the 10992 original data
- V1-V16: trajectory points (x, y coordinate) of the grid
- digits: The digit actually written (the label)


## Source

From A. Izenman (2010) Modern multivariate statistical techniques. Springer.

```
plot.cmdscaleE S3 plot method for cmdscaleE
```


## Description

S3 plot method for cmdscaleE

## Usage

```
## S3 method for class 'cmdscaleE'
plot(
        x,
        plot.type = c("confplot"),
        plot.dim = c(1, 2),
        col,
        label.conf = list(label = TRUE, pos = 3, col = 1, cex = 0.8),
        identify = FALSE,
        type = "p",
        pch = 20,
        asp = 1,
        main,
        xlab,
        ylab,
        xlim,
        ylim,
        legpos,
    )
```


## Arguments

x
cmdscaleE object
plot.type type of plot
plot.dim dimensions used for plotting
col color
label.conf list of label options
identify boolean flag for interactively identify points
type type of plot
pch plotting character
asp aspect ratio (defaults to 1)
main main title
$x l a b \quad$ label of $x$ axis
ylab label of $y$ axis
$x$ lim limits of $x$ axis
$y \lim \quad$ limits of $y$ axis
legpos position of legend
... additional arguments passed to plot

## Details

This function duplicates the plot method for smacof so it can be used with cmdscaleE objects. See plot.smacof for the arguments.

## Value

No return value, just plots a 'cmdscaleE' object.

```
plot.smacofP S3 plot method for smacofP objects
```


## Description

S3 plot method for smacofP objects

## Usage

```
## S3 method for class 'smacofP'
plot(
    x,
    plot.type = "confplot",
    plot.dim = c(1, 2),
    bubscale = 5,
    col,
    label.conf = list(label = TRUE, pos = 3, col = 1, cex = 0.8),
    identify = FALSE,
    type = "p",
    pch = 20,
    asp = 1,
    main,
    xlab,
    ylab,
    xlim,
    ylim,
    legend = TRUE,
    legpos,
    loess = TRUE,
)
```


## Arguments

X
plot.type String indicating which type of plot to be produced: "confplot", "resplot", "Shepard", "stressplot","transplot", "bubbleplot" (see details)
plot.dim dimensions to be plotted in confplot; defaults to $\mathrm{c}(1,2)$
bubscale Scaling factor (size) for the bubble plot
col
label.conf
vector of colors for the points
List with arguments for plotting the labels of the configurations in a configuration plot (logical value whether to plot labels or not, label position, label color)

| identify | If 'TRUE', the 'identify()' function is called internally that allows to add configuration labels by mouse click |
| :---: | :---: |
| type | What type of plot should be drawn (see also 'plot') |
| pch | Plot symbol |
| asp | Aspect ratio; defaults to 1 so distances between x and y are represented accurately; can lead to slighlty weird looking plots if the variance on one axis is much smaller than on the other axis; use NA if the standard type of R plot is wanted where the ylim and xlim arguments define the aspect ratio - but then the distances seen are no longer accurate |
| main | plot title |
| xlab | label of x axis |
| ylab | label of $y$ axis |
| $x \mathrm{lim}$ | scale of $x$ axis |
| ylim | scale of y axis |
| legend | Flag whether legends should be drawn for plots that have legends |
| legpos | Position of legend in plots with legends |
| loess | should loess fit be added to Shepard plot |
|  | Further plot arguments passed: see 'plot.smacof' and 'plot' for detailed information. |

## Details

- Configuration plot (plot.type = "confplot"): Plots the MDS configurations.
- Residual plot (plot.type = "resplot"): Plots the dissimilarities against the fitted distances with a linear regression line (without an intercept as in ratio MDS).
- Linearized Shepard diagram (plot.type = "Shepard"): Diagram with the transformed observed dissimilarities against the transformed fitted distance as well as loess curve and a least squares line. The fitted lines do not have an intercept.
- Transformation Plot (plot.type = "transplot"): Diagram with the observed dissimilarities (lighter) and the transformed observed dissimilarities (darker) against the fitted distances together with the nonlinear regression curve (no intercept). Works for 1 mds or bcStress models too, but is somewhat nonsensical due to them being energy models.
- Stress decomposition plot (plot.type = "stressplot"): Plots the stress contribution in of each observation. Note that it rescales the stress-per-point (SPP) from the corresponding smacof function to percentages (sum is 100). The higher the contribution, the worse the fit. Only implemented for models from the classical stress world, not for bemds or lmds (throws an error).
- Bubble plot (plot.type = "bubbleplot"): Combines the configuration plot with the point stress contribution. The larger the bubbles, the better the fit.Only implemented for models from the classical stress world, bemds or lmds (throws an error).


## Value

no return value; just plot for class 'smacofP' (see details)

```
plot.stops S3 plot method for stops objects
```


## Description

S3 plot method for stops objects

## Usage

\#\# S3 method for class 'stops'
plot(x, plot.type = c("confplot"), main, asp = NA, ...)

## Arguments

X
plot.type
main
asp aspect ratio of $x / y$ axis; defaults to NA; setting to 1 will lead to an accurate represenation of the fitted distances.

Further plot arguments passed: see 'plot.smacof' and 'plot' for detailed information.
Details:

- Configuration plot (plot.type = "confplot"): Plots the MDS configurations.
- Residual plot (plot.type = "resplot"): Plots the dissimilarities against the fitted distances.
- Linearized Shepard diagram (plot.type = "Shepard"): Diagram with the transformed observed dissimilarities against the transformed fitted distance as well as loess smooth and a least squares line.
- Stress decomposition plot (plot.type = "stressplot", only for SMACOF objects in $\$$ fit): Plots the stress contribution in of each observation. Note that it rescales the stress-per-point (SPP) from the corresponding smacof function to percentages (sum is 100). The higher the contribution, the worse the fit.
- Bubble plot (plot.type = "bubbleplot", only available for SMACOF objects \$fit): Combines the configuration plot with the point stress contribution. The larger the bubbles, the better the fit.


## Value

no return value, just plots

```
plot3d.cmdscaleE S3 plot3d method for class cmdscaleE
```


## Description

This methods produces a dynamic 3D configuration plot.

```
Usage
    ## S3 method for class 'cmdscaleE'
    plot3d(
        x,
        plot.dim = c(1, 2, 3),
        xlab,
        ylab,
        zlab,
        col,
        main,
        bgpng = NULL,
        ax.grid = TRUE,
        sphere.rgl = FALSE,
    )
```


## Arguments

x

## plot.dim

xlab
ylab
zlab
col color of the text labels
main plot title
bgpng Background image from rgl library; 'NULL' for white background
ax.grid If 'TRUE', axes grid is plotted.
sphere.rgl If 'TRUE', rgl sphere (background) is plotted.
... Further plot arguments passed: see 'plot3d' in package 'rgl' for detailed information.

## Value

No return value, just plots a 'cmdscale' object.

## Description

This methods produces a dynamic 3D configuration plot.

## Usage

```
## S3 method for class 'stops'
plot3d(x, ...)
```


## Arguments

x
...
object of class stops
Further plot arguments to the method of the class of slot \$fit, see plot.smacof or plot3d.cmdscaleE. Also see 'rgl' in package 'rgl'

## Value

no return value, just plots

```
plot3dstatic plot3dstatic: static 3D plots
```


## Description

A static 3d plot S3 generic

## Usage

plot3dstatic(x, plot. $\operatorname{dim}=c(1,2,3)$, main, xlab, ylab, zlab, col, ...)

## Arguments

x
plot.dim dimensions to plot
main main title
$\mathrm{xlab} \quad$ label for x axis
ylab label for $y$ axis
zlab label for z axis
col color
... other arguments

## Details

## A static 3d plot

## Value

No return value, just plots.

```
plot3dstatic.cmdscaleE
    3D plots: plot3dstatic method for class cmdscaleE
```


## Description

This methods produces a static 3D configuration plot.

## Usage

```
## S3 method for class 'cmdscaleE'
plot3dstatic(x, plot.dim = c(1, 2, 3), main, xlab, ylab, zlab, col, ...)
```


## Arguments

x
plot.dim vector of length 3 with dimensions to be plotted
main plot title
$x$ lab label of x axis
ylab label of $y$ axis
zlab label of $z$ axis
col color of the text labels
... Further plot arguments passed: see 'scatterplot3d' in package 'scatterplot3d' for detailed information.

## Value

No return value, just plots a 'cmdscaleE' object.

## Description

This methods produces a static 3D configuration plot.

## Usage

\#\# S3 method for class 'stops'
plot3dstatic (x, ...)

## Arguments

x
object of class stops
Further plot arguments to the method of the class of slot fit, see plot3dstatic or plot3dstatic.cmdscaleE. Also see 'scatterplot3d' in package 'scatterplot3d'.

## Value

no return value, just plots

```
    powerStressMin Power Stress SMACOF
```


## Description

An implementation to minimize power stress by minimization-majorization. Usually more accurate but slower than powerStressFast.

## Usage

powerStressMin( delta,
kappa $=1$,
lambda $=1$,
nu = 1,
weightmat $=1-\operatorname{diag}(n r o w(d e l t a))$,
init = NULL,
ndim $=2$,
acc $=1 \mathrm{e}-10$,
itmax = 50000,
verbose = FALSE
)

## Arguments

delta dist object or a symmetric, numeric data.frame or matrix of distances
kappa power of the transformation of the fitted distances; defaults to 1
lambda the power of the transformation of the proximities; defaults to 1
nu the power of the transformation for weightmat; defaults to 1
weightmat a matrix of finite weights
init starting configuration
ndim dimension of the configuration; defaults to 2
acc numeric accuracy of the iteration
itmax maximum number of iterations. Defaults to 50000.
verbose should iteration output be printed; if $>1$ then yes

## Value

an object of class 'smacofP' (inheriting form 'smacofB', see smacofSym). It is a list with the components

- delta: Observed dissimilarities, not normalized
- obsdiss: Observed transformed dissimilarities, not normalized
- confdist: Configuration dissimilarities, NOT normalized
- conf: Matrix of fitted configuration, NOT normalized
- stress: Default stress (stress 1; sqrt of explicitly normalized stress)
- spp: Stress per point (based on stress.en)
- ndim: Number of dimensions
- model: Name of smacof model
- niter: Number of iterations
- nobj: Number of objects
- type: Type of MDS model
- weightmat: weighting matrix
- pars: hyperparameter vector theta
and some additional components
- stress.m: default stress is the explicitly normalized stress on the normalized, transformed dissimilarities
- deltaorig: observed, untransformed dissimilarities
- kappa: kappa parameter
- lambda: lambda parameter
- nu: nu parameter (aka rho)


## Note

The functionality related to power stress and the 'smacofP' class is also available in the 'cops' package. Expect masking when both are loaded.

## Author(s)

Jan de Leeuw \& Thomas Rusch

## See Also

```
smacofSym
```


## Examples

```
dis<-smacof::kinshipdelta
res<-powerStressMin(as.matrix(dis),kappa=2,lambda=1.5,nu=2,
    weightmat=as.matrix(dis/2),itmax=1000)
res
summary(res)
plot(res)
```

print.cmdscale S3 print method for cmdscale

## Description

S3 print method for cmdscale

## Usage

\#\# S3 method for class 'cmdscale' print(x, ...)

## Arguments

x cmdscale object
... additional arguments

## Value

No return value, just prints.
print.sammon

Description
S3 print method for sammon objects

## Usage

```
## S3 method for class 'sammon'
print(x, ...)
```


## Arguments

| $x$ | cmdscale object |
| :--- | :--- |
| $\ldots$ | additional arguments |

## Value

No return value, just prints.

```
print.stops S3 print method for stops objects
```


## Description

S3 print method for stops objects

## Usage

\#\# S3 method for class 'stops'
print(x, ...)

## Arguments

x stops object
... additional arguments

## Value

no return value, just prints
print.summary.smacofP S3 print method for summary.smacofP

## Description

S3 print method for summary.smacofP

## Usage

\#\# S3 method for class 'summary.smacofP'
print(x, ...)

## Arguments

x object of class summary.smacofP
... additional arguments

## Value

No return value, just prints a 'summary.smacofP'

$$
\text { print.summary.stops } \quad \text { S3 print method for summary.stops }
$$

## Description

S3 print method for summary.stops

## Usage

\#\# S3 method for class 'summary.stops'
print(x, ...)

## Arguments

x
object of class summary.stops
... additional arguments

## Value

no return value, just prints
procruster
procruster: a procrustes function

## Description

procruster: a procrustes function

## Usage

procruster(x)

## Arguments

x mumeric matrix

## Value

A double or complex matrix.

```
    residuals.stops S3 residuals method for stops
```


## Description

S3 residuals method for stops

## Usage

```
## S3 method for class 'stops'
    residuals(object, ...)
```


## Arguments

| object | object of class stops |
| :--- | :--- |
| $\ldots$ | addditional arguments |

## Value

a vector of residuals (observed minus fitted distances)

## Description

Wrapper to sammon for S3 class

## Usage

sammon(d, y = NULL, $k=2, \ldots$ )

## Arguments

d a distance structure such as that returned by 'dist' or a full symmetric matrix. Data are assumed to be dissimilarities or relative distances, but must be positive except for self-distance. This can contain missing values.
y An initial configuration. If NULL, 'cmdscale' is used to provide the classical solution. (If there are missing values in 'd', an initial configuration must be provided.) This must not have duplicates.
$k \quad$ The dimension of the configuration
... Additional parameters passed to sammon, see sammon

## Details

overloads MASS::sammon and adds class attributes for which there are methods. The functionality is duplicated in the cops package.

## Value

An object of class 'sammonE' that inherits from sammon. This function only adds an extra slot to the list with the call, adds column labels to the \$points and assigns S3 classes 'sammonE', 'cmdscale'. It also adds a slot obsdiss with normalized dissimilarities.

```
secularEq Secular Equation
```


## Description

Secular Equation

## Usage

secularEq(a, b)

## Arguments

| a | matrix |
| :---: | :---: |
| b | matrix |
| sqdist | Squared distances |

## Description

Squared distances

## Usage

sqdist(x)

## Arguments

x
numeric matrix

## Value

a matrix of squared distances
stoploss Calculate the weighted multiobjective loss function used in STOPS

## Description

Calculate the weighted multiobjective loss function used in STOPS

## Usage

```
stoploss(
    obj,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
        "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(-1/length(structures), length(structures)),
    strucpars,
    type = c("additive", "multiplicative"),
    verbose = 0
)
```


## Arguments

obj
object returned inside a stop_* function. Uses the stress.m slot for getting the stress.
stressweight weight to be used for the fit measure; defaults to 1
structures which c-structuredness indices to be included in the loss
strucweight the weights of the structuredness indices; defaults to -1/\#number of structures
strucpars a list of parameters to be passed to the c-structuredness indices in the same order as the values in structures. If the index has no parameters or you want to use the defaults, supply NULL. (alternatively a named list that has the structure name as the element name).
type what type of weighted combination should be used? Can be 'additive' or 'multiplicative'.
verbose verbose output

## Value

a list with calculated stoploss (\$stoploss), structuredness indices (\$strucinidices) and hyperparameters (\$parameters and \$theta)

```
stops stops: structure optimized proximity scaling
```


## Description

A package for "structure optimized proximity scaling" (STOPS), a collection of methods that fit nonlinear distance transformations in multidimensional scaling (MDS) and trade-off the fit with structure considerations to find optimal parameters or optimal configurations. The package contains various functions, wrappers, methods and classes for fitting, plotting and displaying different MDS models in a STOPS framework like Torgerson scaling, SMACOF, Sammon mapping, elastic scaling, symmetric SMACOF, spherical SMACOF, sstress, rstress, powermds, power elastic scaling, power sammon mapping, power stress, Isomap, approximate power stress, restricted power stress. All of these models can also be fit as MDS variants (i.e., no structuredness). The package further contains functions for optimization (Adaptive Luus-Jaakola and for Bayesian optimization with treed Gaussian process with jump to linear models) and functions for various structuredness indices This allows to fit STOPS models as described in Rusch, Mair, Hornik (2023).

## Usage

```
stops(
    dis,
    loss = c("strain", "stress", "smacofSym", "powerstress", "powermds", "powerelastic",
        "powerstrain", "elastic", "sammon", "sammon2", "smacofSphere", "powersammon",
            "rstress", "sstress", "isomap", "isomapeps", "bcstress", "lmds", "apstress",
            "rpowerstress"),
```

```
    theta = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
        "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
        "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    ndim = 2,
    weightmat = NULL,
    init = NULL,
    stressweight = 1,
    strucweight,
    strucpars,
optimmethod = c("SANN", "ALJ", "pso", "Kriging", "tgp", "DIRECT", "stogo", "cobyla",
    "crs2lm", "isres", "mlsl", "neldermead", "sbplx", "hjk", "cmaes"),
    lower,
    upper,
    verbose = 0,
    type = c("additive", "multiplicative"),
    initpoints = 10,
    itmax = 50,
    itmaxps = 10000,
    model,
    control,
)
```


## Arguments

dis numeric matrix or dist object of a matrix of proximities
loss which loss function to be used for fitting, defaults to stress.
theta hyperparameter vector starting values for the transformation functions. If the length is smaller than the number of hyperparameters for the MDS version the vector gets recycled (see the corresponding stop_XXX function or the vignette for how theta must look like exactly for each loss). If larger than the number of hyperparameters for the MDS method, an error is thrown. If completely missing theta is set to 1 and recycled.
structures character vector of which c-structuredness indices should be considered; if missing no structure is considered.
ndim number of dimensions of the target space
weightmat (optional) a matrix of nonnegative weights; defaults to 1 for all off diagonals
init
(optional) initial configuration
stressweight weight to be used for the fit measure; defaults to 1
strucweight vector of weights to be used for the c-structuredness indices (in the same order as in structures); defaults to $-1 /$ length(structures) for each index
strucpars (possibly named with the structure). Metaparameters for the structuredness indices (gamma in the article). It's safest for it be a list of lists with the named arguments for the structuredness indices and the order of the lists must be like the
order of structures. So something like this list(list(par1Struc1=par1Struc1, par2Struc1=par2Str where parYStrucX are the named arguments for the metaparameter $Y$ of the structure X the list elements corresponds to. For a structure without parameters, set NULL. Parameters in different list elements parYStrucX can have the same name. For example, say we want to use cclusteredness with metaparameters epsilon=10 and $\mathrm{k}=4$ (and the default for the other parameters), cdependence with no metaparameters and cfaithfulness with metaparameter $k=7$ one would list(list(epsilon=10, $\mathrm{k}=4$ ), list(NULL), list(dis=obdiss, $\mathrm{k}=6$ )) for structures vector ("cclusteredness","cdependence","cfaithfulness"). The parameter lists must be in the same ordering as the indices in structures. If missing it is set to NULL and defaults are used. It is also possible to supply a structure's metaparameters as a list of vectors with named elements if the metaparameters are scalars, so like list(c(par1Struc1=parStruc1, par2Struc1=par1Struc1, ...) , c(par1Struc2=p That can have unintended consequences if the metaparameter is a vector or matrix.
optimmethod What solver to use. Currently supported are Bayesian optimization with Gaussian Process priors and Kriging ("Kriging"), Bayesian optimization with treed Gaussian processes with jump to linear models ("tgp"), Adaptive LJ Search ("ALJ"), Particle Swarm optimization ("pso"), simulated annealing ("SANN"), "DIRECT", Stochastic Global Optimization ("stogo"), COBYLA ("cobyla"), Controlled Random Search 2 with local mutation ("crs2lm"), Improved Stochastic Ranking Evolution Strategy ("isres"), Multi-Level Single-Linkage ("mlsl"), Nelder-Mead ("neldermead"), Subplex ("sbplx"), Hooke-Jeeves Pattern Search ("hjk"), CMA-ES ("cmaes"). Defaults to "ALJ" version. tgp, ALJ, Kriging and pso usually work well for relatively low values of itmax.
lower The lower contraints of the search region. Needs to be a numeric vector of the same length as the parameter vector theta.
upper The upper contraints of the search region. Needs to be a numeric vector of the same length as the parameter vector theta.
verbose numeric value hat prints information on the fitting process; $>2$ is very verbose.
type
initpoints
itmax maximum number of iterations of the outer optimization (for theta) or number of steps of Bayesian optimization; default is 50 . We recommend a higher number for ALJ (around 150). Note that due to the inner workings of some solvers, this may or may not correspond to the actual number of function evaluations performed (or PS models fitted). E.g., with tgp the actual number of function evaluation of the PS method is between itmax and $6 *$ itmax as tgp samples 16 candidates from the posterior and uses the best candidate. For pso it is the number of particles s times itmax. For cmaes it is usually a bit higher than itmax. This currently may get overruled by a control argument if it is used (and then set to either ewhat is supplie dby control or to the default of the method).
itmaxps maximum number of iterations of the inner optimization (to obtain the PS configuration)
model a character specifying the surrogate model to use. For Kriging it specifies the covariance kernel for the GP prior; see covTensorProduct-class defaults to "powerexp". For tgp it specifies the non stationary process used see bgp, defaults to "btgpllm"
control a control argument passed to the outer optimization procedure. Will override any other control arguents passed, especially verbose and itmax. For the efect of control, see the functions pomp::sannbox for SANN and pso::psoptim for pso, cmaes::cma_es for cmaes, dfoptim::hjkb for hjk and the nloptr docs for the algorithms DIRECT, stogo, cobyla, crs2lm, isres, mlsl, neldermead, sbplx.
. . additional arguments passed to the outer optimization procedures (not fully tested).

## Details

The stops package provides five categories of important functions:
Models \& Algorithms:

- stops() ... which fits STOPS models as described in Rusch et al. (2023). By setting cordweight or strucweight to zero they can also be used to fit metric MDS for many different models, see below.
- powerStressMin()... a workhorse for fitting many stresses, including s-stress, r-stress (De Leeuw, 2014), Sammon mapping with power transformations (powersammon), elastic scaling with power transformation (powerelastic), power stress. They can most conveniently be accessed via the stops functions and setting stressweight $=1$ and cordweight or strucweight $=0$ or by the dedicated functions starting with stop_foo where foo is the method and setting stressweight $=1$ and strucweight $=0$. It uses the nested majorization algorithm for r-stress of De Leeuw(2014).
- bcStressMin()... a workhorse for fitting Box-Cox stress (Chen \& Buja, 2013).
- $\operatorname{lmds}() . .$. a workhorse for the local MDS of Chen \& Buja (2008).

Structuredness Indices: Various c-structuredness as c_foo(), where foo is the name of the structuredness. See Rusch et al. (2023).
Optimization functions:

- ljoptim() ... An (adaptive) version of the Luus-Jakola random search

Wrappers and convenience functions:

- conf_adjust(): procrustes adjustment of configurations
- cmdscale(), sammon(): wrappers that return S3 objects
- stop_smacofSym(), stop_sammon(), stop_cmdscale(), stop_rstress(), stop_powerstress(),stop_smacofSphere(), stop_sammon2(), stop_elastic(), stop_sstress(), stop_powerelastic(), stop_powersammon(), stop_powermds(), stop_isomap(), stop_isomapeps(), stop_bcstress(), stop_lmds(), stop_apstress(),stops_rpowerstress(): stop versions of these MDS models.
- stoploss() ... a function to calculate stoploss (Rusch et al., 2023)

Methods: For most of the objects returned by the high-level functions S3 classes and methods for standard generics were implemented, including print, summary, plot, plot3d, plot3dstatic.

## References:

- Rusch, T., Mair, P., \& Hornik, K. (2023). Structure-based hyperparameter selection with Bayesian optimization in multidimensional scaling. Statistics \& Computing, 33, [28]. https://doi.org/10.1007/s11222-022-10197-w

Authors: Thomas Rusch, Lisha Chen, Jan de Leeuw, Patrick Mair, Kurt Hornik
Maintainer: Thomas Rusch
The combination of c-structurednes indices and stress uses the stress.m values, which are the explictly normalized stresses. Reported however is the stress-1 value which is sqrt(stress.m).

## Value

A list with the components

- stoploss: the stoploss value
- optim: the object returned from the optimization procedure
- stressweight: the stressweight
- strucweight: the vector of structure weights
- call: the call
- optimmethod: The solver selected
- losstype: The PS badness-of-fit function
- nobj: the number of objects in the configuration
- type: The type of stoploss scalacrisation (additive or multiplicative)
- fit: The fitted PS object (most importantly $\$$ fit\$conf the fitted configuration)


## Examples

```
data(kinshipdelta,package="smacof")
strucpars<-list(list(epsilon=10,minpts=2, scale=3),list(NULL))
dissm<-as.matrix(kinshipdelta)
#STOPS with strain
resstrain<-stops(dissm,loss="strain", theta=1, structures=c("cclusteredness", "cdependence"),
strucpars=strucpars,optimmethod="ALJ",lower=0,upper=10,itmax=10)
resstrain
summary(resstrain)
plot(resstrain)
#STOPS with stress
strucpars<-list(list(epsilon=10,minpts=2,scale=3),NULL)
resstress<-stops(dissm,loss="stress",
structures=c("cclusteredness","cdependence"),
strucpars=strucpars,optimmethod="ALJ",lower=0,upper=10)
resstress
summary(resstress)
plot(resstress)
plot(resstress,"Shepard")
```

```
#STOPS with powerstress
respstress<-stops(dissm,loss="powerstress",
structures=c("cclusteredness","cdependence"),
strucpars=strucpars,weightmat=dissm,
itmaxps=1000,optimmethod="ALJ",lower=c(0,0,1),upper=c(10,10,10))
respstress
summary(respstress)
plot(respstress)
#STOPS with bcstress
resbcstress<-stops(dissm,loss="bcstress",
structures=c("cclusteredness","cdependence"),
strucpars=strucpars,optimmethod="ALJ",lower=c (0,1,0), upper=c (10,10,10))
resbcstress
summary(resbcstress)
plot(resbcstress)
#STOPS with lmds
reslmds<-stops(dissm,loss="lmds",
structures=c("cclusteredness","clinearity"),
strucpars=strucpars,optimmethod="ALJ",lower=c(2,0),upper=c(10,2))
reslmds
summary(reslmds)
plot(reslmds)
#STOPS with Isomap (the epsilon version)
resiso<-stops(dissm,loss="isomapeps",
structures=c("cclusteredness","clinearity"),
strucpars=strucpars,optimmethod="ALJ",lower=70,upper=120)
resiso
summary(resiso)
plot(resiso)
data(kinshipdelta,package="smacof")
strucpar<-list(NULL,NULL) #parameters for indices
res1<-stops(kinshipdelta,loss="stress",
structures=c("cclumpiness","cassociation"),strucpars=strucpar,
lower=0, upper=10,itmax=10)
res1
data(BankingCrisesDistances)
strucpar<-list(c(epsilon=10,minpts=2),NULL) #parameters for indices
res1<-stops(BankingCrisesDistances[,1:69],loss="stress",verbose=0,
structures=c("cclusteredness","clinearity"),strucpars=strucpar,
lower=0, upper=10)
res1
strucpar<-list(list(alpha=0.6,C=15,var.thr=1e-5,zeta=NULL),
list(alpha=0.6,C=15,var.thr=1e-5,zeta=NULL))
res1<-stops(BankingCrisesDistances[,1:69],loss="stress",verbose=0,
```

```
structures=c("cfunctionality","ccomplexity"),strucpars=strucpar,
lower=0, upper=10)
res1
```

stop_apstress STOPS version of approximated power stress models.

## Description

This uses an approximation to power stress that can make use of smacof as workhorse. Free parameters are tau and upsilon.

## Usage

```
stop_apstress(
    dis,
    theta = c(1, 1),
    ndim = 2,
    weightmat = NULL,
    init = NULL,
    itmax = 1000,
    ...,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
        "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
        "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities <br> theta <br> the theta vector of parameters to optimize over. Must be of length two, with <br> the first the tau argument and the second the upsilon argument. It can also be <br> a scalar of the tau and upsilon transformation for the observed proximities and <br> gets recycled for both ups and tau (so they are equal). Defaults to 11. |
| :--- | :--- |
| ndim | number of dimensions of the target space |
| weightmat | (optional) a binary matrix of nonnegative weights |
| init | (optional) initial configuration |
| itmax | number of iterations. default is 1000. |


| $\ldots$. | additional arguments to be passed to the fitting procedure |
| :--- | :--- |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | a character vector listing the structure indices to use. They always are called <br> "cfoo" with foo being the structure. |
| strucweight | weight to be used for the structures; defaults to $1 /$ number of structures <br> a list of list of parameters for the structuredness indices; each list element cor- <br> responds to one index in the order of the appearance in structures vector. See <br> examples. |
| verbose | numeric value hat prints information on the fitting process; >2 is extremely ver- <br> bose <br> which weighting to be used in the multi-objective optimization? Either 'addi- |
| type | tive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress 1 (sqrt stress.m)
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa=1, tau, ups)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object


## Description

STOPS version of Box Cox Stress

## Usage

```
stop_bcstress(
    dis,
    theta \(=c(1,1,0)\),
    weightmat \(=\) NULL,
    init = NULL,
    ndim = 2,
    itmax \(=5000\),
    ...,
    stressweight = 1 ,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
```

```
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
    "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
    "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; the first is mu (for the fitted distances), the second lambda (for the proximities), the third nu (for the weights). If a scalar is given it is recycled. Defaults to 110 . |
| weightmat | (not used) |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structures to look for |
| strucweight | weight to be used for the structures; defaults to 0.5 |
| strucpars | a list of parameters for the structuredness indices; each list element corresponds to one index in the order of the appeacrance in structures |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | which weighting to be used in the multi-objective optimization? Either 'additive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa, lambda)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
    stop_cmdscale STOPS version of strain
```


## Description

The free parameter is lambda for power transformations of the observed proximities.

## Usage

```
stop_cmdscale(
    dis,
    theta \(=1\),
    weightmat \(=\) NULL,
    ndim \(=2\),
    init \(=\) NULL,
    ...,
    stressweight = 1 ,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose \(=0\),
    type = c("additive", "multiplicative"),
    itmax = NULL
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; this must be a scalar of the lambda transformation for the observed proximities. |
| weightmat | (optional) a matrix of nonnegative weights. Not used. |
| ndim | number of dimensions of the target space |
| init | (optional) initial configuration |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to $1 / \#$ number of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |


| type | How to construct the target function for the multi objective optimization? Either <br> 'additive' (default) or 'multiplicative' |
| :--- | :--- |
| itmax | placeholder for compatibility in stops call; not used |

## Value

A list with the components

- stress: Sqrt of explicitly normalized stress.
- stress.m: explictly normalized stress
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_elastic STOPS versions of elastic scaling models (via smacofSym)
```


## Description

The free parameter is lambda for power transformations the observed proximities. The fitted distances power is internally fixed to 1 and the power for the weights=delta is -2 . Allows for a weight matrix because of smacof.

## Usage

```
    stop_elastic(
        dis,
        theta = 1,
        ndim = 2,
        weightmat = NULL,
        init = NULL,
        itmax = 1000,
        ...,
        stressweight = 1,
        structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
        "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose = 0,
        type = c("additive", "multiplicative")
    )
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; this must be a scalar of the lambda transformation for the observed proximities. Defaults to 1 . |
| ndim | number of dimensions of the target space |
| weightmat | (optional) a matrix of nonnegative weights (NOT the elscal weights) |
| init | (optional) initial configuration |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to $1 / \# n u m b e r$ of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | How to construct the target function for the multi objective optimization? Either 'additive' (default) or 'multiplicative' |

## Value

A list with the components

- stress: the stress-1 (sqrt(stress.m))
- stress.m: default normalized stress (used for STOPS)
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj objects
stop_isomap1 STOPS version of isomap to optimize over integer $k$.


## Description

Free parameter is k.

## Usage

```
stop_isomap1(
    dis,
    theta \(=3\),
    weightmat \(=\) NULL,
    ndim \(=2\),
    init \(=\) NULL,
    stressweight = 1 ,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose = 0,
        type = c("additive", "multiplicative"),
        itmax = NULL
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the number of shortest dissimilarities retained for a point (nearest neighbours), the isomap parameter. Must be a numeric scalar. Defaults to 3 . |
| weightmat | (optional) a matrix of nonnegative weights |
| ndim | number of dimensions of the target space |
| init | (optional) initial configuration |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to $1 / \#$ number of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | How to construct the target function for the multi objective optimization? Either 'additive' (default) or 'multiplicative' |
| itmax | placeholder for compatibility in stops call; not used |

## Details

Currently this version is a bit less flexible than the vegan one, as the only allowed parameter for isomap is the theta ( k in isomap, no epsilon) and the shortest path is always estimated with argument "shortest". Also note that fragmentedOK is always set to TRUE which means that for theta that is too small only the largest conected group will be analyzed. If that's not wanted just set the theta higher.

## Value

A list with the components

- stress: Not really stress but 1-GOF where GOF is the first element returned from cmdscale (the sum of the first ndim absolute eigenvalues divided by the sum of all absolute eigenvalues).
- stress.m: default normalized stress (sqrt explicitly normalized stress; really the stress this time)
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object


## Description

Free parameter is eps.

## Usage

```
stop_isomap2(
    dis,
    theta = stats::quantile(dis, 0.1),
    weightmat = NULL,
    ndim = 2,
    init = NULL,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative"),
    itmax = NULL
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the number of shortest dissimilarities retained for a point (neighbourhood region), the isomap parameter. Defaults to the 0.1 quantile of the empirical distribution of dis. |
| weightmat | (optional) a matrix of nonnegative weights |
| ndim | number of dimensions of the target space |
| init | (optional) initial configuration |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to 1/\#number of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | How to construct the target function for the multi objective optimization? Either 'additive' (default) or 'multiplicative' |
| itmax | placeholder for compatibility in stops call; not used |

## Details

Currently this version is a bit less flexible than the vegan one, as the only allowed parameter for isomap is the theta (epsilon in isomap) and the shortest path is always estimated with argument "shortest". Also note that fragmentedOK is always set to TRUE which means that for theta that is too small only the largest conected group will be analyzed. If that's not wanted just set the theta higher.

## Value

A list with the components

- stress: Not really stress but 1-GOF where GOF is the first element returned from cmdscale (the sum of the first ndim absolute eigenvalues divided by the sum of all absolute eigenvalues).
- stress.m: default normalized stress (sqrt explicitly normalized stress; really the stress this time)
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_lmds STOPS version of lMDS
```


## Description

STOPS version of 1MDS

## Usage

```
stop_lmds(
    dis,
    theta = c(2, 0.5),
    weightmat = NULL,
    init = NULL,
    ndim = 2,
    itmax = 5000,
    ...,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; the first is k (for the neighbourhood), the second tau (for the penalty). If a scalar is given it is recycled. Defaults to 2 and 0.5 . |
| weightmat | (not used) |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structures to look for |
| strucweight | weight to be used for the structures; defaults to 0.5 |
| strucpars | a list of parameters for the structuredness indices; each list element corresponds to one index in the order of the appeacrance in structures |


| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely ver- <br> bose |
| :--- | :--- |
| type | which weighting to be used in the multi-objective optimization? Either 'addi- <br> tive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa, lambda)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_powerelastic STOPS version of elastic scaling with powers for proximities and dis-
tances
```


## Description

This is power stress with free kappa and lambda but rho is fixed to -2 and the weights are delta.

## Usage

```
stop_powerelastic(
    dis,
    theta \(=c(1,1,-2)\),
    weightmat \(=\) NULL,
    init \(=\) NULL,
    ndim \(=2\),
    itmax \(=1 \mathrm{e}+05\),
    ...,
    stressweight \(=1\),
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose \(=0\),
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; a vector of length two where the first element is kappa (for the fitted distances), the second lambda (for the observed proximities). If a scalar for the free parameters is given it is recycled. Defaults to 11 . |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which strcutures to look for |
| strucweight | weight to be used for the structures; defaults to 0.5 |
| strucpars | a list of parameters for the structuredness indices; each list element corresponds to one index in the order of the appeacrance in structures |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | which weighting to be used in the multi-objective optimization? Either 'additive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa, lambda)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object


## Description

This is power stress with free kappa and lambda but rho is fixed to 1 , so no weight transformation.

## Usage

```
stop_powermds(
    dis,
    theta \(=c(1,1)\),
    weightmat = NULL,
    init = NULL,
    ndim \(=2\),
    itmax \(=1 \mathrm{e}+05\),
    ...,
    stressweight = 1 ,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
            "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose \(=0\),
        type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; a vector of length 2 where the first element is kappa (for the fitted distances), the second lambda (for the observed proximities). If a scalar is given it is recycled. Defaults to 1 . |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structures to look for |
| strucweight | weight to be used for the structures; defaults to 0.5 |
| strucpars | a list of parameters for the structuredness indices; each list element corresponds to one index in the order of the appeacrance in structures |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | which weighting to be used in the multi-objective optimization? Either 'additive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa, lambda)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object


## Description

This is power stress with free kappa and lambda but rho is fixed to -1 and the weights are delta.

```
Usage
    stop_powersammon(
        dis,
        theta = c(1, 1),
        weightmat = NULL,
        init = NULL,
        ndim = 2,
        itmax = 1e+05,
        ...,
        stressweight = 1,
        structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
        "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose = 0,
        type = c("additive", "multiplicative")
)
```


## Arguments

\(\left.$$
\begin{array}{ll}\text { dis } & \begin{array}{l}\text { numeric matrix or dist object of a matrix of proximities } \\
\text { theta }\end{array}
$$ <br>
the theta vector of powers; a vector of length two where the first element is kappa <br>
(for the fitted distances), the second lambda (for the observed proximities). If a <br>

scalar is given it is recycled for the free parameters. Defaults to 11 .\end{array}\right]\)| (optional) a matrix of nonnegative weights |
| :--- |
| weightmat |
| init |


| ndim | number of dimensions of the target space |
| :--- | :--- |
| itmax | number of iterations |
| $\ldots$ | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structures to look for |
| strucweight | weight to be used for the structures; defaults to 0.5 <br> strucpars |
| a list of parameters for the structuredness indices; each list element corresponds <br> to one index in the order of the appeacrance in structures |  |
| verbose | numeric value hat prints information on the fitting process; >2 is extremely ver- <br> bose <br> which weighting to be used in the multi-objective optimization? Either 'addi- |
| type | tive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa, lambda)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_powerstress STOPS version of powerstress
```


## Description

Power stress with free kappa and lambda and rho.

## Usage

```
stop_powerstress(
    dis,
    theta = c(1, 1, 1),
    weightmat = NULL,
    init = NULL,
    ndim = 2,
    itmax = 10000,
    ...,
    stressweight = 1,
```

```
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
        "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
        "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; the first is kappa (for the fitted distances), the second lambda (for the observed proximities), the third nu (for the weights). If a scalar is given it is recycled. Defaults to 111 . |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | a character vector listing the structure indices to use. They always are called "cfoo" with foo being the structure. |
| strucweight | weight to be used for the structures; defaults to $1 /$ number of structures |
| strucpars | a list of parameters for the structuredness indices; each list element corresponds to one index in the order of the appeacrance in structures |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | which weighting to be used in the multi-objective optimization? Either 'additive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa, lambda, nu)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object


## Description

## STOPS version of restricted powerstress

## Usage

```
stop_rpowerstress(
    dis,
    theta = c(1, 1, 1),
    weightmat = NULL,
    init = NULL,
    ndim = 2,
    itmax = 10000,
    ...,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; the first two arguments are for kappa and lambda and should be equal (for the fitted distances and observed proximities), the third nu (for the weights). Internally the kappa and lambda are equated. If a scalar is given it is recycled (so all elements of theta are equal); if a vector of length 2 is given, it gets expanded to $c($ theta[1],theta[1],theta[2]). Defaults to 111 . |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations. default is 10000 . |
|  | additional arguments to be passed to the fitting procedure powerStressMin |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | a character vector listing the structure indices to use. They always are called "cfoo" with foo being the structure. |


| strucweight | weight to be used for the structures; defaults to $1 /$ number of structures |
| :--- | :--- |
| strucpars | a list of list of parameters for the structuredness indices; each list element cor- <br> responds to one index in the order of the appearance in structures vector. See <br> examples. |
| verbose | numeric value hat prints information on the fitting process; > $>2$ is extremely ver- <br> bose |
| type | which weighting to be used in the multi-objective optimization? Either 'addi- <br> tive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- struc: the structuredness indices
- parameters: the parameters used for fitting (kappa=lambda, nu)
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_rstress STOPS version of rstress
```


## Description

Free parameter is kappa for the fitted distances.

## Usage

```
stop_rstress(
    dis,
    theta \(=1\),
    weightmat \(=\) NULL,
    init \(=\) NULL,
    ndim \(=2\),
    itmax \(=1 \mathrm{e}+05\),
    ...,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
        "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
        "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
```

```
        verbose = 0,
        type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; this must be a scalar of the kappa transformation for the fitted distances proximities. Defaults to 1 . Note the kappa here differs from Jan's version where the parameter was called $r$ and the relationship is $r=k a p p a / 2$ or kappa $=2$ r. |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| ndim | number of dimensions of the target space |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to $1 / \#$ number of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | How to construct the target function for the multi objective optimization? Either 'additive' (default) or 'multiplicative' |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object
stop_sammon STOPS version of Sammon mapping


## Description

Uses MASS::sammon. The free parameter is lambda for power transformations of the observed proximities. The fitted distances power is internally fixed to 1 and the power for the weights=delta is -1 .

## Usage

```
stop_sammon(
    dis,
    theta = 1,
    ndim = 2,
    init = NULL,
    weightmat = NULL,
    itmax = 1000,
    ...,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
    "chierarchy", "cconvexity", "cstriatedness", "coutlying", "cskinniness", "csparsity",
            "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose = 0,
        type = c("additive", "multiplicative")
    )
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities <br> the theta vector of powers; this must be a scalar of the lambda transformation <br> for the observed proximities. Defaults to 1. |
| :--- | :--- |
| ndim | number of dimensions of the target space <br> (optional) initial configuration |
| init | a matrix of nonnegative weights. Has no effect here. <br> weightmat <br> itmax |
| number of iterations |  |
| f. | additional arguments to be passed to the fitting procedure |
| structures | weight to be used for the fit measure; defaults to 1 |
| which structuredness indices to be included in the loss |  |
| strucweight | weight to be used for the structuredness indices; ; defaults to $1 / \#$ number of <br> structures |


| strucpars | the parameters for the structuredness indices |
| :--- | :--- |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely ver- <br> bose |
| type | How to construct the target function for the multi objective optimization? Either <br> 'additive' (default) or 'multiplicative' |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_sammon2
Another STOPS version of Sammon mapping models (via smacofSym)
```


## Description

Uses Smacof, so it can deal with a weight matrix too. The free parameter is lambda for power transformations of the observed proximities. The fitted distances power is internally fixed to 1 and the power for the weights=delta is -1 .

## Usage

```
stop_sammon2(
    dis,
    theta \(=1\),
    ndim \(=2\),
    weightmat \(=\) NULL,
    init = NULL,
    itmax \(=1000\),
    ....
    stressweight = 1 ,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose \(=0\),
        type = c("additive", "multiplicative")
    )
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; this must be a scalar of the lambda transformation for the observed proximities. Defaults to 1. |
| ndim | number of dimensions of the target space |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to $1 / \#$ number of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | How to construct the target function for the multi objective optimization? Either 'additive' (default) or 'multiplicative'. |

## Value

A list with the components

- stress: the stress-1 (sqrt(stress.m))
- stress.m: default normalized stress (used for STOPS)
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object
stop_smacofSphere STOPS versions of smacofSphere models


## Description

The free parameter is lambda for power transformations the observed proximities. The fitted distances power is internally fixed to 1 and the power for the weights is 1 .

## Usage

```
stop_smacofSphere(
    dis,
    theta = 1,
    ndim = 2,
    weightmat = NULL,
    init = NULL,
    itmax = 1000,
    ...,
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
            "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
            "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
        strucweight = rep(1/length(structures), length(structures)),
        strucpars,
        verbose = 0,
        type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector of powers; this must be a scalar of the lambda transformation for the observed proximities. Defaults to 1 . |
| ndim | number of dimensions of the target space |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |
| itmax | number of iterations |
|  | additional arguments to be passed to the fitting procedure |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss |
| strucweight | weight to be used for the structuredness indices; ; defaults to 1/\#number of structures |
| strucpars | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; $>2$ is extremely verbose |
| type | How to construct the target function for the multi objective optimization? Either 'additive' (default) or 'multiplicative' |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object

```
stop_smacofSym STOPS version of smacofSym models
```


## Description

The free parameter is lambda for power transformations the observed proximities. The fitted distances power is internally fixed to 1 and the power for the weights is 1 .

## Usage

```
stop_smacofSym(
    dis,
    theta = 1,
    ndim = 2,
    weightmat = NULL,
    init = NULL,
    itmax = 1000,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
    "chierarchy", "cconvexity", "cstriatedness", "coutlying", "cskinniness", "csparsity",
            "cstringiness", "cclumpiness", "cinequality"),
    stressweight = 1,
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities |
| :---: | :---: |
| theta | the theta vector; must be a scalar for the lambda (proximity) transformation. Defaults to 1 . |
| ndim | number of dimensions of the target space |
| weightmat | (optional) a matrix of nonnegative weights |
| init | (optional) initial configuration |


| itmax | number of iterations |
| :--- | :--- |
| $\ldots$ | additional arguments to be passed to the fitting |
| structures | which structuredness indices to be included in the loss |
| stressweight | weight to be used for the fit measure; defaults to 1 <br> weight to be used for the structuredness indices; ; defaults to 1/\#number of <br> structures |
| strucweight | the parameters for the structuredness indices |
| verbose | numeric value hat prints information on the fitting process; > $>2$ is extremely ver- <br> bose <br> type |
| How to construct the target function for the multi objective optimization? Either <br> 'additive' (default) or 'multiplicative' |  |

## Value

A list with the components

- stress: the stress-1 (sqrt(stress.m))
- stress.m: default normalized stress (used for STOPS)
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stops object


## Description

Free parameter is lambda for the observed proximities. Fitted distances are transformed with power 2, weights have exponent of 1 . Note that the lambda here works as a multiplicator of 2 (as sstress has $f\left(\operatorname{delta}^{\wedge} 2\right)$ ).

## Usage

stop_sstress( dis, theta $=1$, weightmat $=$ NULL, init = NULL, ndim $=2$, itmax $=1 \mathrm{e}+05$,

```
    stressweight = 1,
    structures = c("cclusteredness", "clinearity", "cdependence", "cmanifoldness",
    "cassociation", "cnonmonotonicity", "cfunctionality", "ccomplexity", "cfaithfulness",
        "cregularity", "chierarchy", "cconvexity", "cstriatedness", "coutlying",
        "cskinniness", "csparsity", "cstringiness", "cclumpiness", "cinequality"),
    strucweight = rep(1/length(structures), length(structures)),
    strucpars,
    verbose = 0,
    type = c("additive", "multiplicative")
)
```


## Arguments

| dis | numeric matrix or dist object of a matrix of proximities <br> the theta vector of powers; this must be a scalar of the lambda transformation <br> for the observed proximities. Defaults to 1. Note that the lambda here works as <br> a multiplicator of 2 (as sstress has f(delta^2)). <br> (optional) a matrix of nonnegative weights <br> (optional) initial configuration |
| :--- | :--- |
| weightmat |  |
| the number of dimensions of the target space |  |
| init | ndim |
| itmax | number of iterations |
| additional arguments to be passed to the fitting procedure |  |
| stressweight | weight to be used for the fit measure; defaults to 1 |
| structures | which structuredness indices to be included in the loss <br> weight to be used for the structuredness indices; ; defaults to $1 / \# n u m b e r ~ o f ~$ |
| strucweight | structures <br> the parameters for the structuredness indices |
| strucpars | numeric value hat prints information on the fitting process; $>2$ is extremely ver- <br> berbose |
| type | How to construct the target function for the multi objective optimization? Either <br> 'additive' (default) or 'multiplicative' |

## Value

A list with the components

- stress: the stress
- stress.m: default normalized stress
- stoploss: the weighted loss value
- indices: the values of the structuredness indices
- parameters: the parameters used for fitting
- fit: the returned object of the fitting procedure
- stopobj: the stopobj object
summary.cmdscale S3 summary method for cmdscale


## Description

S3 summary method for cmdscale

## Usage

\#\# S3 method for class 'cmdscale'
summary(object, ...)

## Arguments

$$
\begin{array}{ll}
\text { object } & \text { object of class cmdscale } \\
\ldots & \text { additional arguments }
\end{array}
$$

## Value

No return value, just prints.
summary. sammon S3 summary method for sammon

## Description

S3 summary method for sammon

## Usage

\#\# S3 method for class 'sammon'
summary (object, ...)

## Arguments

$$
\begin{array}{ll}
\text { object } & \text { object of class sammon } \\
\ldots & \text { additional arguments }
\end{array}
$$

## Value

No return value, just prints.
summary.smacofP S3 summary method for smacofP

## Description

S3 summary method for smacofP

## Usage

\#\# S3 method for class 'smacofP'
summary(object, ...)

## Arguments

object object of class smacofP
... additional arguments

## Value

an object of class summary.smacofP
summary.stops S3 summary method for stops

## Description

S3 summary method for stops

## Usage

\#\# S3 method for class 'stops'
summary (object, ...)

## Arguments

| object | object of class stops |
| :--- | :--- |
| $\ldots$ | addditional arguments |

## Value

object of class 'summary.stops'
Swissroll Swiss roll

## Description

A swiss roll data example where 150 data points are arranged on a swiss roll embedded in a 3 D space.

## Usage

data(Swissroll)

## Format

A data frame with 150 rows and 4 columns

## Details

A data frame with the variables (columns)

- x The x axis coordinate for each point
- y The $y$ axis coordinate for each point
- z The z axis coordinate for each point
- col a color code for each point with points along the y axis having the same color (based on the viridis palette)
tgpoptim Bayesian Optimization by a (treed) Bayesian Gaussian Process Prior ( with jumps to linear models) surrogate model Essentially a wrapper for the functionality in tgp that has the same slots as optim with defaults for STOPS models.


## Description

Bayesian Optimization by a (treed) Bayesian Gaussian Process Prior (with jumps to linear models) surrogate model Essentially a wrapper for the functionality in tgp that has the same slots as optim with defaults for STOPS models.

## Usage

```
tgpoptim(
    x ,
    fun,
    ...,
    initpoints \(=10\),
    lower,
    upper,
    acc \(=1 \mathrm{e}-08\),
    itmax \(=10\),
    verbose \(=0\),
    model = "bgp"
)
```


## Arguments

x

## fun

... additional arguments to be passed to the function to be optimized
lower The lower contraints of the search region
upper The upper contraints of the search region
acc if the numerical accuracy of two successive target function values is below this, stop the optimization; defaults to $1 \mathrm{e}-8$
itmax maximum number of iterations
verbose numeric value hat prints information on the fitting process; $>2$ is extremely verbose
model which surrogate model class to use (currently uses defaults only, will extend this to tweak the model)

## Value

A list with the components (for compatiility with optim)

- par The position of the optimum in the search space (parameters that minimize the function; argmin fun).
- value The value of the objective function at the optimum (min fun). Note we do not use the last value in the candidate list but the best candidate (which can but need not coincide).
- svalue The value of the surrogate objective function at the optimal parameters
- counts The number of iterations performed at convergence with entries fnction for the number of iterations and gradient which is always NA at the moment
- convergence 0 successful completion by the accd or acc criterion, 1 indicate iteration limit was reached, 99 is a problem
- message is NULL (only for compatibility or future use)
- history the improvement history
- tgpout the output of the tgp model


## Examples

```
    fbana <- function(x) {
    x1 <- x[1]
    x2 <- x[2]
    100 * (x2 - x1 * x1)^2 + (1 - x1)^2
    }
    res1<-tgpoptim(c(-1.2,1), fbana,lower=c(-5,-5), upper=c(5,5), acc=1e-16, itmax=20)
    res1
    fwild <- function (x) 10*sin(0.3*x)*sin(1.3*x^2) + 0.00001*x^4 + 0.2*x+80
    plot(fwild, -50, 50, n = 1000, main = "Bayesian GP Optimization minimizing 'wild function'")
    set.seed(210485)
    res2<-tgpoptim(50, fwild,lower=-50,upper=50,acc=1e-16,itmax=20,model="btgpllm")
    points(res2$par,res2$value,col="red",pch=19)
    res2
```

    torgerson Torgerson scaling
    
## Description

Torgerson scaling

## Usage

```
torgerson(delta, p = 2)
```


## Arguments

```
delta symmetric, numeric matrix of distances
p target space dimensions
```


## Value

a matrix (a Torgerson scaling configuration)

## Index

```
* clustering
    stops,48
* multivariate
    stop_apstress,54
    stop_bcstress, 55
    stop_cmdscale, 57
    stop_elastic,58
    stop_isomap1,59
    stop_isomap2,61
    stop_lmds, 63
    stop_powerelastic,64
    stop_powermds,65
    stop_powersammon, 67
    stop_powerstress,68
    stop_rpowerstress,70
    stop_rstress,71
    stop_sammon,73
    stop_sammon2,74
    stop_smacofSphere,75
    stop_smacofSym, 77
    stop_sstress,78
    stops,48
ace, 19
apStressMin,4
BankingCrisesDistances,5
bcStressMin,6
bgp, 51
c_association,10
c_clumpiness, 11
c_clusteredness,11
c_complexity,13
c_convexity,14
c_dependence, 14
c_faithfulness, 15
c_functionality,16
c_hierarchy, 17
c_inequality, 17
```

c_linearity, 18
c_manifoldness, 19
c_mine, 20
c_nonmonotonicity, 20
c_outlying, 21
c_regularity, 22
c_skinniness, 23
c_sparsity, 24
c_striatedness, 24
c_stringiness, 25
cl_validity, 17
cmds, 8
cmdscale, 8,8
coef.stops, 9
conf_adjust, 9
cordillera, 12, 23
doubleCenter, 26
enorm, 26
hclust, 17
knn_dist, 27
ljoptim, 27
lmds, 29
mine, $10,13,16,21$
mkBmat, 30
mkPower, 31
mkPower2, 31
optics, 12
optim, 28, 83

Pendigits500, 32
plot.cmdscaleE, 32
plot.smacof, 33, 38
plot.smacofP, 34
plot.stops, 36

```
plot3d.cmdscaleE, 37, 38
plot3d.stops,38
plot3dstatic, 38,40
plot3dstatic.cmdscaleE, 39,40
plot3dstatic.stops,40
powerStressMin, 29,40
print.cmdscale, 42
print.sammon,43
print.stops,43
print.summary.smacofP,44
print.summary.stops,44
procruster,45
residuals.stops,45
sammon, 46, 46
scagnostics, 11, 14, 22-25
secularEq,46
smacofSym, 4, 5, 41, 42
sqdist,47
stop_apstress,54
stop_bcstress,55
stop_cmdscale, 57
stop_elastic, 58
stop_isomap1,59
stop_isomap2,61
stop_lmds,63
stop_powerelastic,64
stop_powermds,65
stop_powersammon,67
stop_powerstress,68
stop_rpowerstress,70
stop_rstress,71
stop_sammon,73
stop_sammon2, 74
stop_smacofSphere, 75
stop_smacofSym,77
stop_sstress,78
stoploss,47
stops,48
summary.cmdscale, }8
summary.sammon, }8
summary.smacofP, 81
summary.stops,81
Swissroll, }8
tgpoptim, 82
torgerson, 84
```

