## Package 'disbayes'

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Description Estimation of incidence and case fatality for a chronic disease, given partial information, using a multi-state model. Given data on age-specific mortality and either inci-

dence or prevalence, Bayesian inference is used to estimate the posterior distributions of incidence, case fatality, and functions of these such as prevalence. The methods are de-

scribed in Jackson et al. (2023) <doi:10.1093/jrsssa/qnac015>.

Title Bayesian Multi-State Modelling of Chronic Disease Burden Data

License GPL-3 Encoding UTF-8 LazyData true

Biarch true

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BugReports https://github.com/chjackson/disbayes/issues

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## **Description**

Bayesian evidence synthesis for chronic disease epidemiology

## References

Stan Development Team (2019). RStan: the R interface to Stan. R package version 2.19.2. https://mc-stan.org

ci2num Convert a proportion and credible interval to a numerator and denominator

## Description

Estimate the number of events and denominator that contain roughly equivalent information to an estimate and uncertainty interval for a proportion, by interpreting the estimate and interval as a Beta posterior arising from a vague Beta(0.5,0.5) prior updated with the data consisting of that number and denominator.

## Usage

```
ci2num(est, lower, upper, epsilon = 0.5, denom0 = 1000)
```

ci2num 3

## **Arguments**

est	Point estimate
lower	Lower 95% credible limit
upper	Upper 95% credible limit
epsilon	If any of lower are zero, then they are replaced by the minimum of epsilon and est/2. Similarly values of 1 for upper are replaced by the maximum of 1-epsilon and (1+est)/2.
denom0	Denominator to use as a default when the point estimate is exactly 0 or 1 (which is not compatible with the beta distribution). Should correspond to a guess of the population size used to produce the estimate, which should be no greater than the actual population of the area, and usually less. Should be either a scalar, or a vector of the same length as est (though note if it is a vector, then only the elements where est is 1 or 0 get used).

#### **Details**

Based on fitting a Beta distribution by least squares, using the method provided by the **SHELF** package.

Requires that the estimate and upper and lower limits are all distinct (except that est=0 is allowed and handled specially for convenience, see denom0). Vectors of estimates and limits may be supplied.

### Value

A data frame with elements num and denom corresponding to the supplied estimate and limits.

#### References

Oakley (2020). SHELF: Tools to Support the Sheffield Elicitation Framework. R package version 1.7.0. https://CRAN.R-project.org/package=SHELF

## **Examples**

```
est <- 3.00 / 100
upper <- 3.52 / 100
lower <- 2.60 / 100
ci2num(est, lower, upper)
```

4 conflict\_disbayes

conflict\_disbayes

Conflict p-values

## Description

A test of the hypothesis that the direct data on a disease outcome give the same information about that outcome as an indirect evidence synthesis obtained from a fitted disbayes model. The outcome may be annual incidence, mortality, remission probabilities, or prevalence.

## Usage

```
conflict_disbayes(x, varname)
```

## Arguments

x A fitted disbayes model.

varname Either inc, prev, mort or rem.

#### **Details**

Hierarchical models are not currently supported in this function.

#### Value

A data frame with columns indicating age, gender and area.

p1 is a "one-sided" p-value for the null hypothesis that  $r_{obs} = r_{fit}$  against the alternative that  $r_{obs} > r_{fit}$ ,

p2 is the two-sided p-value for the null hypothesis that  $r_{obs} = r_{fit}$  against the alternative that  $r_{obs}$  is not equal to  $r_{fit}$ ,

where  $r_{obs}$  is the rate informed only by direct data, and  $r_{fit}$  is the rate informed by evidence synthesis. Therefore if the evidence synthesis excludes the direct data, then these are interpreted as "conflict" p-values (see Presanis et al. 2013).

In each case, a small p-value favours the alternative hypothesis.

#### References

Presanis, A. M., Ohlssen, D., Spiegelhalter, D. J. and De Angelis, D. (2013) Conflict diagnostics in directed acyclic graphs, with applications in Bayesian evidence synthesis. Statistical Science, 28, 376-397.

disbayes

Bayesian estimation of chronic disease epidemiology from incomplete data

#### **Description**

Estimates a three-state disease model from incomplete data. It is designed to estimate case fatality and incidence, given data on mortality and at least one of incidence and prevalence. Remission may also be included in the data and modelled.

#### Usage

```
disbayes(
  data,
  inc_num = NULL,
  inc_denom = NULL,
  inc_prob = NULL,
  inc_lower = NULL,
  inc_upper = NULL,
  prev_num = NULL,
  prev_denom = NULL,
 prev_prob = NULL,
  prev_lower = NULL,
  prev_upper = NULL,
 mort_num = NULL,
 mort_denom = NULL,
 mort_prob = NULL,
 mort_lower = NULL,
 mort_upper = NULL,
  rem_num = NULL,
  rem_denom = NULL,
  rem_prob = NULL,
  rem_lower = NULL,
  rem_upper = NULL,
  age = "age",
  cf_model = "smooth",
  inc_model = "smooth",
  rem_model = "const",
  prev_zero = FALSE,
  inc_trend = NULL,
  cf_trend = NULL,
  cf_init = 0.01,
  eqage = 30,
  eqagehi = NULL,
  sprior = c(1, 1, 1),
  hp_fixed = NULL,
  rem_prior = c(1.1, 1),
```

```
inc_prior = c(2, 0.1),
  cf_prior = c(2, 0.1),
  method = "opt",
  draws = 1000,
  iter = 10000,
  stan_control = NULL,
  bias_model = NULL,
)
```

#### **Arguments**

data

Data frame containing some of the variables below. The variables below are provided as character strings naming columns in this data frame. For each disease measure available, one of the following three combinations of variables must be specified:

(1) numerator and denominator (2) estimate and denominator (3) estimate with lower and upper credible limits.

Mortality must be supplied, and at least one of incidence and prevalence. If remission is assumed to be possible, then remission data should also be supplied (see below).

Estimates refer to the probability of having some event within a year, rather than rates. Rates per year r can be converted to probabilities p as p = 1exp(-r)\$, assuming the rate is constant within the year.

For estimates based on registry data assumed to cover the whole population, then the denominator will be the population size.

inc\_num

Numerator for the incidence data, assumed to represent the observed number of new cases within a year among a population of size inc\_denom.

inc\_denom

Denominator for the incidence data.

The function ci2num can be used to convert a published estimate and interval for a proportion to an implicit numerator and denominator.

Note that to include extra uncertainty beyond that implied by a published interval, the numerator and denominator could be multiplied by a constant, for example, multiplying both the numerator and denominator by 0.5 would give the data source half its original weight.

inc\_prob

Estimate of the incidence probability

inc\_lower Lower credible limit for the incidence estimate inc\_upper Upper credible limit for the incidence estimate

prev\_num Numerator for the estimate of prevalence, i.e. number of people currently with

a disease.

prev\_denom

Denominator for the estimate of prevalence (e.g. the size of the survey used to

obtain the prevalence estimate)

Estimate of the prevalence probability prev\_prob

prev\_lower Lower credible limit for the prevalence estimate Upper credible limit for the prevalence estimate prev\_upper

mort\_num Numerator for the estimate of the mortality probability, i.e number of deaths

attributed to the disease under study within a year

mort\_denom Denominator for the estimate of the mortality probability (e.g. the population

size, if the estimates were obtained from a comprehensive register)

mort\_prob Estimate of the mortality probability

mort\_lower Lower credible limit for the mortality estimate mort\_upper Upper credible limit for the mortality estimate

rem\_num Numerator for the estimate of the remission probability, i.e number of people

observed to recover from the disease within a year.

Remission data should be supplied if remission is permitted in the model, either as a numerator and denominator or as an estimate and lower credible interval. Conversely, if no remission data are supplied, then remission is assumed to be impossible. These "data" may represent a prior judgement rather than observation - lower denominators or wider credible limits represent weaker prior information.

rem\_denom Denominator for the estimate of the remission probability

rem\_prob Estimate of the remission probability

rem\_lower Lower credible limit for the remission estimate Upper credible limit for the remission estimate rem\_upper

Variable in the data indicating the year of age. This must start at age zero, but age

can end at any age.

cf\_model Model for how case fatality rate varies with age.

> "smooth" (the default). Case fatality rate is modelled as a smooth function of age, using a spline.

> "indep" Case fatality rates are estimated independently for each year of age. This may be useful for determining how much information is in the data. That is, if the posterior from this model is identical to the prior for a certain age, then there is no information in the data alone about case fatality at that age, indicating that some other structural assumption (such as a smooth function of age) or external data are equired to give more precise estimates.

> "increasing" Case fatality rate is modelled as a smooth and increasing function of age.

"const" Case fatality rate is modelled as constant with age.

inc\_model Model for how incidence rates vary with age.

> "smooth" (the default). Incidence rates are modelled as a smooth spline function of age.

"indep" Incidence rates for each year of age are estimated independently.

Model for how remission rates vary with age, which are typically less wellinformed by data, compared to incidence and case fatality.

"const" (the default). Constant remission rate over all ages.

"smooth" Remission rates are modelled as a smooth spline function of age.

"indep" Remission rates estimated independently over all ages.

rem\_model

prev\_zero

If TRUE, attempt to estimate prevalence at age zero from the data, as part of the Bayesian model, even if the observed prevalence is zero. Otherwise (the default) this is assumed to be zero if the count is zero, and estimated otherwise.

inc trend

Matrix of constants representing trends in incidence through calendar time by year of age. There are nage rows and nage columns, where nage is the number of years of age represented in the data. The entry in the ith row and jth column represents the ratio between the incidence nage+j years prior to the year of the data, year, and the incidence in the year of the data, for a person i-1 years of age. For example, if nage=100 and the data refer to the year 2017, then the first column refers to the year 1918 and the last (100th) column refers to 2017. The last column should be all 1, unless the current data are supposed to be biased.

To produce this format from a long data frame, filter to the appropriate outcome and subgroup, and use pivot\_wider, e.g.

trends <- ihdtrends filter(outcome=="Incidence", gender=="Female")</pre> pivot\_wider(names\_from="year", values\_from="p2017") select(-age, -gender, -outcome) as.matrix()

cf\_trend

Matrix of constants representing trends in case fatality through calendar time by year of age, in the same format as inc\_trend.

cf\_init

Initial guess at a typical case fatality value, for an average age.

egage

Case fatalities (and incidence and remission rates) are assumed to be equal for all ages below this age, inclusive, when using the smoothed model.

eqagehi

Case fatalities (and incidence and remission rates) are assumed to be equal for all ages above this age, inclusive, when using the smoothed model.

sprior

Rates of the exponential prior distributions used to penalise the coefficients of the spline model. The default of 1 should adapt appropriately to the data, but Higher values give stronger smoothing, or lower values give weaker smoothing, if required.

This can be a named vector with names "inc", "cf", "rem" in any order, giving the prior smoothness rates for incidence, case fatality and remission. If any of these are not smoothed they can be excluded, e.g. sprior = c(cf=10, inc=1).

This can also be an unnamed vector of three elements, where the first refers to the spline model for incidence, the second for case fatality, the third for remission. If one of the rates (e.g. remission) is not being modelled with a spline, any number can be supplied here and it is just ignored.

A list with one named element for each hyperparameter to be fixed. The value should be either

- a number (to fix the hyperparameter at this number)
- TRUE (to fix the hyperparameter at the posterior mode from a training run where it is not fixed)

If the element is either NULL, FALSE, or omitted from the list, then the hyperparameter is given a prior and estimated as part of the Bayesian model.

The hyperparameters that can be fixed are

- scf Smoothness parameter for the spline relating case fatality to age.
- sinc Smoothness parameter for the spline relating incidence to age.

hp\_fixed

For example, to fix the case fatality smoothness to 1.2 and fix the incidence smoothness to its posterior mode, specify hp\_fixed = list(scf=1.2, sinc=TRUE).

rem\_prior Vector of two elements giving the Gamma shape and rate parameters of the prior for the remission rate, used in both rem\_model="const" and rem\_model="indep".

Vector of two elements giving the Gamma shape and rate parameters of the prior for the incidence rate. Only used if inc\_model="indep", for each age-specific

rate.

inc\_prior

cf\_prior Vector of two elements giving the Gamma shape and rate parameters of the prior for the case fatality rate. Only used if cf\_model="const", or if cf\_model="indep",

for each age-specific rate, and for the rate at eqage in cf\_model="increasing".

method String indicating the inference method, defaulting to "opt".

If method="mcmc" then a sample from the posterior is drawn using Markov Chain Monte Carlo sampling, via **rstan**'s rstan::sampling() function. This is the most accurate but the slowest method.

If method="opt", then instead of an MCMC sample from the posterior, disbayes returns the posterior mode calculated using optimisation, via **rstan**'s **rstan**::optimizing() function. A sample from a normal approximation to the (real-line-transformed) posterior distribution is drawn in order to obtain credible intervals.

If the optimisation fails to converge (non-zero return code), try increasing the number of iterations from the default 1000, e.g. disbayes(..., iter=10000, ...), or changing the algorithm to disbayes(..., algorithm="Newton", ...).

If there is an error message that mentions chol, then the computed Hessian matrix is not positive definite at the reported optimum, hence credible intervals cannot be computed. This can occur either because of numerical error in computation of the Hessian, or because the reported optimum is wrong. If you are willing to believe the optimum and live without credible intervals, then set draws=0 to skip computation of the Hessian. To examine the problematic Hessian, set hessian=TRUE, draws=0, then look at the fithessian component of the disbayes return object. If it can be inverted, do sqrt(diag(solve())) on the Hessian, and check for NaNs, indicating the problematic parameters. Otherwise, diagonal entries of the Hessian matrix that are very small may indicate parameters that are poorly identified from the data, leading to computational problems.

If method="vb", then variational Bayes methods are used, via **rstan**'s **rstan**: vb() function. This is labelled as "experimental" by **rstan**. It might give a better approximation to the posterior than method="opt", but has not been investigated much for disbayes models.

Number of draws from the normal approximation to the posterior when using method="opt".

Number of iterations for MCMC sampling, or maximum number of iterations for optimization.

(method="mcmc" only). List of options supplied as the control argument to rstan::sampling() in **rstan** for the main model fit.

Experimental model for bias in the incidence estimates due to conflicting information between the different data sources. If bias\_model=NULL (the default)

draws

iter

stan\_control

bias\_model

1

no bias is assumed, and all data are assumed to be generated from the same age-specific incidences.

Otherwise there are assumed to be two alternative curves of incidence by age (denoted 2 and 1) where curve 2 is related to curve 1 via a constant hazard ratio that is estimated from the data, given a standard normal prior on the log scale. Three distinct curves would not be identifiable from the data.

If bias\_model="inc" then the incidence data is assumed to be generated from curve 2, and the prevalence and mortality data from curve 1.

bias\_model="prev" then the prevalence data is generated from curve 2, and the incidence and mortality data from curve 1.

If bias\_model="incprev" then both incidence and prevalence data are generated from curve 2, and the mortality data from curve 1.

Further arguments passed to rstan::sampling() to control MCMC sampling, or rstan::optimizing() to control optimisation, in Stan.

#### Value

A list including the following components

call: Function call that was used.

fit: An object containing posterior samples from the fitted model, in the stanfit format returned by the stan function in the **rstan** package.

method: Optimisation method that was chosen.

nage: Number of years of age in the data

dat: A list containing the input data in the form of numerators and denominators.

stan\_data: Full list of data supplied to Stan

stan\_inits: Full list of parameter initial values supplied to Stan

hp\_fixed Values of any hyperparameters that are fixed during the main model fit.

Use the tidy.disbayes method to return summary statistics from the fitted models, simply by calling tidy() on the fitted model.

#### References

Jackson C, Zapata-Diomedi B, Woodcock J. (2023) "Bayesian multistate modelling of incomplete chronic disease burden data" Journal of the Royal Statistical Society, Series A, 186(1), 1-19 doi:10.1093/jrsssa/qnac015

disbayes\_hier Bayesian estimation of chronic disease epidemiology from incomplete data - hierarchical model for case fatalities.

### **Description**

A variant of disbayes in which data from different areas can be related in a hierarchical model and, optionally, the effect of gender can be treated as additive with the effect of area. This is much more computationally intensive than the basic model in disbayes. Time trends are not supported in this function.

## Usage

```
disbayes_hier(
  data,
  group,
  gender = NULL,
  inc_num = NULL,
  inc_denom = NULL,
  inc_prob = NULL,
  inc_lower = NULL,
  inc_upper = NULL,
  prev_num = NULL,
  prev_denom = NULL,
  prev_prob = NULL,
  prev_lower = NULL,
  prev_upper = NULL,
 mort_num = NULL,
 mort_denom = NULL,
 mort_prob = NULL,
 mort_lower = NULL,
 mort_upper = NULL,
  rem_num = NULL,
  rem_denom = NULL,
  rem_prob = NULL,
  rem_lower = NULL,
  rem_upper = NULL,
  age = "age",
  cf_init = 0.01,
  eqage = 30,
  eqagehi = NULL,
  cf_model = "default",
  inc_model = "smooth",
  rem_model = "const",
  prev_zero = FALSE,
  sprior = c(1, 1, 1),
  hp_fixed = NULL,
  nfold_int_guess = 5,
  nfold_int_upper = 100,
  nfold_slope_guess = 5,
  nfold\_slope\_upper = 100,
  mean_int_prior = c(0, 10),
 mean\_slope\_prior = c(5, 5),
```

```
gender_int_priorsd = 0.82,
  gender_slope_priorsd = 0.82,
  inc_prior = c(1.1, 0.1),
  rem_prior = c(1.1, 1),
  method = "opt",
  draws = 1000,
  iter = 10000,
  stan_control = NULL,
)
```

#### **Arguments**

data

Data frame containing some of the variables below. The variables below are provided as character strings naming columns in this data frame. For each disease measure available, one of the following three combinations of variables must be specified:

(1) numerator and denominator (2) estimate and denominator (3) estimate with lower and upper credible limits.

Mortality must be supplied, and at least one of incidence and prevalence. If remission is assumed to be possible, then remission data should also be supplied (see below).

Estimates refer to the probability of having some event within a year, rather than rates. Rates per year r can be converted to probabilities p as p = 1exp(-r)\$, assuming the rate is constant within the year.

For estimates based on registry data assumed to cover the whole population, then the denominator will be the population size.

group

Variable in the data representing the area (or other grouping factor).

gender

If NULL (the default) then the data are one homogenous gender, and there should be one row per year of age. Otherwise, set gender to a character string naming the variable in the data representing gender (or other categorical grouping factor). Gender will then treated as a fixed additive effect, so the linear effect of gender on log case fatality is the same in each area. The data should have one row per year of age and gender.

inc\_num

Numerator for the incidence data, assumed to represent the observed number of new cases within a year among a population of size inc\_denom.

inc\_denom

Denominator for the incidence data.

The function ci2num can be used to convert a published estimate and interval for a proportion to an implicit numerator and denominator.

Note that to include extra uncertainty beyond that implied by a published interval, the numerator and denominator could be multiplied by a constant, for example, multiplying both the numerator and denominator by 0.5 would give the data source half its original weight.

Estimate of the incidence probability

inc\_lower

Lower credible limit for the incidence estimate Upper credible limit for the incidence estimate

inc\_upper

inc\_prob

Numerator for the estimate of prevalence, i.e. number of people currently with prev\_num a disease. Denominator for the estimate of prevalence (e.g. the size of the survey used to prev\_denom obtain the prevalence estimate) prev\_prob Estimate of the prevalence probability Lower credible limit for the prevalence estimate prev\_lower prev\_upper Upper credible limit for the prevalence estimate Numerator for the estimate of the mortality probability, i.e number of deaths mort\_num attributed to the disease under study within a year mort\_denom Denominator for the estimate of the mortality probability (e.g. the population size, if the estimates were obtained from a comprehensive register) Estimate of the mortality probability mort\_prob mort\_lower Lower credible limit for the mortality estimate mort\_upper Upper credible limit for the mortality estimate Numerator for the estimate of the remission probability, i.e number of people rem\_num observed to recover from the disease within a year. Remission data should be supplied if remission is permitted in the model, either as a numerator and denominator or as an estimate and lower credible interval. Conversely, if no remission data are supplied, then remission is assumed to be impossible. These "data" may represent a prior judgement rather than observation - lower denominators or wider credible limits represent weaker prior information. rem\_denom Denominator for the estimate of the remission probability rem\_prob Estimate of the remission probability rem\_lower Lower credible limit for the remission estimate rem\_upper Upper credible limit for the remission estimate Variable in the data indicating the year of age. This must start at age zero, but age can end at any age. Initial guess at a typical case fatality value, for an average age. cf\_init Case fatalities (and incidence and remission rates) are assumed to be equal for eqage all ages below this age, inclusive, when using the smoothed model. egagehi Case fatalities (and incidence and remission rates) are assumed to be equal for all ages above this age, inclusive, when using the smoothed model. cf\_model The following alternative models for case fatality are supported: "default" (the default). Random intercepts and slopes, and no further restriction. "interceptonly". Random intercepts, but common slopes.

"increasing". Case fatality is assumed to be an increasing function of age (note it is constant below "eqage" in all models) with a common slope for all

"common" Case fatality is an unconstrained function of age which is common to all areas, i.e. it has the same parameter values in every area. This and

groups.

"increasing\_common" are used in situations where you want to compare a model with area-specific rates with a single model for the data aggregated over areas. Modelling the area-disaggregated data using a common function for all areas is equivalent to a model for the aggregated data, and can be statistically compared (using cross-validation) with a model with area-specific rates.

"increasing\_common" Case fatality is an increasing function of age which is common to all areas.

"const" Case fatality is assumed to be constant with age, for all ages, but different in each area.

"const\_common" Case fatality is a constant over all ages and areas.

In all models, case fatality is a smooth function of age.

inc\_model

Model for how incidence varies with age.

"smooth" (the default). Incidence is modelled as a smooth spline function of age, independently for each area (and gender).

"indep" Incidence rates for each year of age, area (and gender) are estimated independently.

rem\_model

Model for how remission varies with age. Currently supported models are "const" for a constant remission rate over all ages, "const" for a smooth spline, or "indep" for a different remission rates estimated independently for each age with no smoothing.

prev\_zero

If TRUE, attempt to estimate prevalence at age zero from the data, as part of the Bayesian model, even if the observed prevalence is zero. Otherwise (the default) this is assumed to be zero if the count is zero, and estimated otherwise.

sprior

Rates of the exponential prior distributions used to penalise the coefficients of the spline model. The default of 1 should adapt appropriately to the data, but Higher values give stronger smoothing, or lower values give weaker smoothing, if required.

This can be a named vector with names "inc", "cf", "rem" in any order, giving the prior smoothness rates for incidence, case fatality and remission. If any of these are not smoothed they can be excluded, e.g. sprior = c(cf=10, inc=1).

This can also be an unnamed vector of three elements, where the first refers to the spline model for incidence, the second for case fatality, the third for remission. If one of the rates (e.g. remission) is not being modelled with a spline, any number can be supplied here and it is just ignored.

hp\_fixed

A list with one named element for each hyperparameter to be fixed. The value should be either

- a number (to fix the hyperparameter at this number)
- TRUE (to fix the hyperparameter at the posterior mode from a training run where it is not fixed)

If the element is either NULL, FALSE, or omitted from the list, then the hyperparameter is given a prior and estimated as part of the Bayesian model.

The hyperparameters that can be fixed are

- scf Smoothness parameter for the spline relating case fatality to age.
- sinc Smoothness parameter for the spline relating incidence to age.

• scfmale Smoothness parameter for the spline defining how the gender effect relates to age. Only for models with additive gender and area effects.

- sd\_int Standard deviation of random intercepts for case fatality.
- sd\_slope Standard deviation of random slopes for case fatality.

For example, to fix the case fatality smoothness to 1.2, fix the incidence smoothness to its posterior mode, and estimate all the other hyperparameters, specify hp\_fixed = list(scf=1.2, sinc=TRUE).

nfold\_int\_guess

Prior guess at the ratio of case fatality between a high risk (97.5% quantile) and low risk (2.5% quantile) area.

nfold\_int\_upper

Prior upper 95% credible limit for the ratio in average case fatality between a high risk (97.5% quantile) and low risk (2.5% quantile) area.

nfold\_slope\_guess, nfold\_slope\_upper

This argument and the next argument define the prior distribution for the variance in the random linear effects of age on log case fatality. They define a prior guess and upper 95% credible limit for the ratio of case fatality slopes between a high trend (97.5% quantile) and low risk (2.5% quantile) area. (Note that the model is not exactly linear, since departures from linearity are defined through a spline model. See the Jackson et al. paper for details.).

mean\_int\_prior Vector of two elements giving the prior mean and standard deviation respectively for the mean random intercept for log case fatality.

mean\_slope\_prior

Vector of two elements giving the prior mean and standard deviation respectively for the mean random slope for log case fatality.

gender\_int\_priorsd

Prior standard deviation for the additive effect of gender on log case fatality gender\_slope\_priorsd

Prior standard deviation for the additive effect of gender on the linear age slope of log case fatality

inc\_prior

Vector of two elements giving the Gamma shape and rate parameters of the prior for the incidence rate. Only used if inc\_model="indep", for each age-specific rate.

rem\_prior

Vector of two elements giving the Gamma shape and rate parameters of the prior for the remission rate, used in both rem\_model="const" and rem\_model="indep".

method

String indicating the inference method, defaulting to "opt".

If method="mcmc" then a sample from the posterior is drawn using Markov Chain Monte Carlo sampling, via **rstan**'s rstan::sampling() function. This is the most accurate but the slowest method.

If method="opt", then instead of an MCMC sample from the posterior, disbayes returns the posterior mode calculated using optimisation, via **rstan**'s rstan::optimizing() function. A sample from a normal approximation to the (real-line-transformed) posterior distribution is drawn in order to obtain credible intervals.

If the optimisation fails to converge (non-zero return code), try increasing the number of iterations from the default 1000, e.g. disbayes(..., iter=10000, ...), or changing the algorithm to disbayes(..., algorithm="Newton", ...).

If there is an error message that mentions chol, then the computed Hessian matrix is not positive definite at the reported optimum, hence credible intervals cannot be computed. This can occur either because of numerical error in computation of the Hessian, or because the reported optimum is wrong. If you are willing to believe the optimum and live without credible intervals, then set draws=0 to skip computation of the Hessian. To examine the problematic Hessian, set hessian=TRUE, draws=0, then look at the \$fit\$hessian component of the disbayes return object. If it can be inverted, do sqrt(diag(solve())) on the Hessian, and check for NaNs, indicating the problematic parameters. Otherwise, diagonal entries of the Hessian matrix that are very small may indicate parameters that are poorly identified from the data, leading to computational problems.

If method="vb", then variational Bayes methods are used, via **rstan**'s **rstan**: vb() function. This is labelled as "experimental" by **rstan**. It might give a better approximation to the posterior than method="opt", but has not been investigated much for disbayes models.

draws Number of draws from the normal approximation to the posterior when using

method="opt".

iter Number of iterations for MCMC sampling, or maximum number of iterations

for optimization.

stan\_control (method="mcmc" only). List of options supplied as the control argument to

rstan::sampling() in rstan for the main model fit.

... Further arguments passed to rstan::sampling() to control MCMC sampling,

or rstan::optimizing() to control optimisation, in Stan.

#### Value

A list including the following components

call: Function call that was used.

fit: An object containing posterior samples from the fitted model, in the stanfit format returned by the stan function in the **rstan** package.

method: Optimisation method that was chosen.

nage: Number of years of age in the data

narea: Number of areas (or other grouping variable that defines the hierarchical model).

ng: Number of genders (or other categorical variable whose effect is treated as additive with the area effect).

groups: Names of the areas (or other grouping variable), taken from the factor levels in the original data.

genders: Names of the genders (or other categorical variable), taken from the factor levels in the original data.

dat: A list containing the input data in the form of numerators and denominators.

stan\_data: Full list of data supplied to Stan

stan\_inits: Full list of parameter initial values supplied to Stan

trend: Whether a time trend was modelled

hp\_fixed Values of any hyperparameters that are fixed during the main model fit.

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#### References

Jackson C, Zapata-Diomedi B, Woodcock J. "Bayesian multistate modelling of incomplete chronic disease burden data" https://arxiv.org/abs/2111.14100

ihdengland

Ischemic heart disease in England

## **Description**

Ischemic heart disease in England

## Usage

ihdengland

#### **Format**

A data frame with columns:

sex: "male" or "female".

ageyr. Year of age.

location. Name of the location, which is either a city region or region in England.

num\_mort. Numerator behind the estimate of mortality

num\_inc. Numerator behind the estimate of incidence

num\_prev. Numerator behind the estimate of prevalence

denom\_mort. Denominator behind the estimate of mortality

denom\_inc. Denominator behind the estimate of incidence

denom\_prev. Denominator behind the estimate of prevalence

#### **Details**

The data were processed to

- \* change the geography to refer to England city regions and the remaining English regions,
- \* change counts by 5-year age groups to estimated 1-year counts,
- \* obtain estimated numerators and denominators from the published point estimates and uncertainty intervals. A point estimate of the risk is equivalent to the numerator divided by the denominator. The denominator is related to the extent of uncertainty around this estimate, and obtained using the Bayesian method implemented in ci2num.

The script given in https://github.com/chjackson/disbayes/blob/master/data-raw/gbd\_process.Rmd shows these steps.

#### Source

Global Burden of Disease, 2017

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#### References

Jackson C, Zapata-Diomedi B, Woodcock J. "Bayesian multistate modelling of incomplete chronic disease burden data" https://arxiv.org/abs/2111.14100.

ihdtrends

Trends in ischemic heart disease in England

#### **Description**

Trends in ischemic heart disease in England

## Usage

ihdtrends

#### **Format**

A data frame with columns:

gender: "male" or "female".

age: Year of age. year: Calendar year.

p2017: Estimated ratio between the outcome in the calendar year and the outcome in 2017.

outcome: Outcome referred to (incidence or case fatality).

#### **Details**

The data were interpolated and smoothed to produce a matrix by year of age and calendar year, using the script at https://github.com/chjackson/disbayes/blob/master/data-raw/trends.r.

#### Source

Scarborough, P., Wickramasinghe, K., Bhatnagar, P. and Rayner, M. (2011) Trends in coronary heart disease, 1961-2001. British Heart Foundation.

Smolina, K., Wright, F. L., Rayner, M. and Goldacre, M. J. (2012) Determinants of the decline in mortality from acute myocardial infarction in England between 2002 and 2010: linked national database study. BMJ, 344.

British Heart Foundation (2020) Heart and Circulatory Disease Statistics 2020. British Heart Foundation.

loo.disbayes 19

loo.disbayes	Leave-one-out cross validation for disbayes models	

## Description

Leave-one-out cross validation for disbayes models

## Usage

```
## S3 method for class 'disbayes'
loo(x, outcome = "overall", ...)
```

## **Arguments**

X	A model fitted by disbayes. Any of the computation methods are supported.
outcome	Either "overall", to assess the fit to all data, or one of "inc", "prev", "mort" or "rem", to assess the fit to the incidence data, prevalence data, mortalidy data or remission data, respectively.
	Other arguments (currently unused).

#### Value

An object of class "loo" as defined by the loo package.

### See Also

loo\_indiv to return tidied observation-specific contributions to the overall model fit computed here.

loo_indiv	Extract observation-specific contributions from a disbayes leave-one- out cross validation

## **Description**

Extract observation-specific contributions from a disbayes leave-one-out cross validation

## Usage

```
loo_indiv(x, agg = FALSE)
looi_disbayes(x, agg = FALSE)
```

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#### **Arguments**

agg

x For loo\_indiv, an object returned by loo.disbayes. For looi\_disbayes, an object returned by disbayes.

object returned by drabbayes.

If TRUE then the observation-specific contributions are aggregated over outcome type, returning a data frame with one row for each of incidence, prevalence, mortality and remission (if remission is included in the model), and one column

for each of "elpd\_loo", "p\_loo" and "looic".

#### Value

A data frame with one row per observed age-specific mortality, incidence, prevalence and/or remission age-specific data-point, containing leave-one-out cross validation statistics representing how well the model would predict that observation if it were left out of the fit.

These are computed with the **loo** package.

loo\_indiv acts on the objects that are returned by running loo on disbayes objects. looi\_disbayes acts directly on disbayes objects. Both of those functions return a data frame with LOO contributions for each data point.

#### **Functions**

 looi\_disbayes(): Observation-level leave-one-out cross validation statistics for a disbayes model

plot.disbayes

Quick and dirty plot of estimates from disbayes models against age

#### **Description**

Posterior medians and 95

## Usage

```
## S3 method for class 'disbayes'
plot(x, variable = "cf", ...)
```

## **Arguments**

x Object returned by disbayes

variable Name of the variable of interest to plot against age, by default case fatality rates.

... Other arguments. Currently unused

## Value

A ggplot2 object that can be printed to show the plot, or customised by adding geoms.

Better plots can be drawn by tidying the object returned by disbayes, and using ggplot2 directly on the tidy data frame that this produces. See the vignette for examples.

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plot.disbayes\_hier

Quick plot of estimates from hierarchical disbayes models against age

#### **Description**

Posterior medians and 95% credible intervals for a quantity of interest are plotted against year of age.

## Usage

```
## S3 method for class 'disbayes_hier'
plot(x, variable = "cf", ci = FALSE, ...)
```

## **Arguments**

x Object returned by disbayes\_hier

variable Name of the variable of interest to plot against age, by default case fatality rates.

ci Show 95% credible intervals with ribbons.

... Other arguments. Currently unused

#### Value

A ggplot2 object that can be printed to show the plot, or customised by adding geoms.

Better plots can be drawn by tidying the object returned by disbayes, and using ggplot2 directly on the tidy data frame that this produces. See the vignette for examples.

## **Description**

Create tidy data for a check of observed against fitted outcome probability estimates from disbayes

#### **Usage**

```
plotfit_data_disbayes(x)
```

## **Arguments**

Х

Fitted model from disbayes

### Value

A data frame containing observed data in the form of outcome probabilities, as extracted by tidy\_obsdat, and estimates of the corresponding probability parameters from the fitted model.

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plotfit_disbayes	Graphical check of observed against fitted outcome probabilities from disbayes
------------------	--

## **Description**

The data behind the plot can be produced using plotfit\_data\_disbayes, to enable customised plots to be produced by hand with ggplot2.

## Usage

```
plotfit_disbayes(x, agemin = 50)
```

## **Arguments**

x Fitted model from disbayes

agemin Minimum age to show on the horizontal axis.

#### Value

A ggplot2 object containing the plot.

tidy.disbayes

Form a tidy data frame from the estimates from a disbayes fit

## **Description**

```
Simply call this after fitting disbayes, as, e.g.
```

```
res <- disbayes(...)
tidy(res)</pre>
```

## Usage

```
## S3 method for class 'disbayes'
tidy(x, startyear = 1, ...)
## S3 method for class 'disbayes_hier'
tidy(x, ...)
```

## Arguments

x Object returned by disbayes

Startyear Only used for models with time trends. Numeric year represented by year 1 in

the data. For example, set this to 1918 to convert years 1-100 to years 1918-

2017.

Other arguments (currently unused)

tidy.disbayes 23

#### Value

A data frame with one row per model parameter, giving summary statistics for the posterior distribution for that parameter. For array parameters, e.g. those that depend on age or area, then the age and area are returned in separate columns, to make it easier to summarise and plot the results, e.g. using **ggplot2**.

Model parameters might include, depending on the model specification,

- cf, inc, rem: Case fatality, incidence, remission rates
- inc\_prob, rem\_prob, mort\_prob, cf\_prob: Annual incidence, remission, mortality and case fatality risks (probabilities).
- prev\_prob Prevalence (probability).
- state\_probs State occupancy probabilities.
- beta, beta\_inc Coefficients of the spline basis for case fatality and incidence respectively.
- lambda\_cf, lambda\_inc Smoothness parameters of the spline functions.
- prevzero Prevalence at age zero
- cfbase Case fatality at the baseline age (only in models where case fatality is increasing).
- dcf Annual increments in case fatality (only in models where case fatality is increasing).
- bias\_loghr Log hazard ratio describing bias in case fatality between datasets (only in models where bias\_model has been set).

#### For models with time trends:

• cf\_yr, inc\_yr, state\_probs\_yr Case fatality rates, incidence rates and state occupancy probabilities in years prior to the current year. cf and inc refer to the rates for the current year, the one represented in the data.

#### Only for hierarchical models:

- mean\_inter, mean\_slope,sd\_inter,sd\_slope. Mean and standard deviation for random effects distribution for the intercept and slope of log case fatality.
- lambda\_cf\_male, lambda\_inc\_male. Smoothness of the additive gender effect on case fatality and incidence.
- bareat Area-level contribution to spline basis coefficients.
- barea Normalised spline basis coefficients.

#### **Functions**

• tidy(disbayes\_hier): Tidy method for hierarchical disbayes models

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tidy\_obsdat

Extract observed data from a disbayes model fit

## Description

Extract observed data from a disbayes model fit

## Usage

tidy\_obsdat(x)

## **Arguments**

Х

Fitted disbayes model

## Value

A data frame with columns num and denom giving the incidence, prevalence and mortality (and remission if used) numerators and denominators used in the model fit. The column var indicates which of incidence, prevalence etc. the numbers refer to. The column prob is derived as num divided by denom. Columns lower and upper define credible intervals for the "data-based" point estimate prob, obtained from the Beta posterior assuming a Beta(0.5, 0.5) prior.

This "data-based" point estimate can be compared with estimates from the model using the functions plotfit\_data\_disbayes and plotfit\_disbayes.

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