# Package 'cdfquantreg' 

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cdfquantreg-package

## Description

Employs a two-parameter family of distributions for modelling random variables on the $(0,1)$ interval by applying the cumulative distribution function (cdf) of one parent distribution to the quantile function of another.

## Details

Package: cdfquantreg
Type: Package
Date: 2022-05-19
License: GPL-3

The cdfquantreg package includes 36 members of a two-parameter family of distributions for modelling random variables on the $(0,1)$ interval (see cdfqrFamily). This family has explicit pdfs, cdfs, and quantile functions. The two parameters consist of a location parameter and a dispersion parameter. The location parameter models the median and the dispersion parameter models the spread of other quantiles around the median (see Smithson and Shou, 2016, for details about the distribution family and the models). Separate submodels may be specified for the location and for the dispersion parameters, permitting different or overlapping sets of predictors in each.
The package offers maximum likelihood (see cdfquantreg) and bootstrap (see qrBoot) estimation methods. All model functions return S3 objects. In addition to the usual goodness of fit information, the package provides root-mean-squared errors in both the raw and logit scales, and the gradient. Model diagnostics include raw, Pearson, and deviance residuals (see residuals.cdfqr), and dfbetas (see influence.cdfqr).
For each distribution, the package provides evaluations of the $\mathrm{pdf}(\mathrm{dq}), \mathrm{cdf}(\mathrm{pq})$, and quantile ( qq ), as well as random samples from any of them (rq). Evaluations of skew and kurtosis (qrPwlm) also are available using probability-weighted L-moments.

## Author(s)

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## References

Shou, Y. and Smithson, M., (2019). cdfquantreg: An R Package for CDF-Quantile Regression. Journal of Statistical Software,88(1), pp.1-30, doi: 10.18637/jss.v088.i01

## See Also

cdfarFamily
Ambdata Ambiguity-Conflict data

## Description

A data from a study that investigates the judgment under ambiguity and conflict

## Usage

Ambdata

## Format

A data frame with 166 rows and 2 variables:
ID subject ID
value Rating in each judgment scenario
scenario Index for judgment scenarios

## Source

https://pubmed.ncbi.nlm.nih.gov/16594767/

```
anova.cdfqr Model comparison test for fitted cdfqr models
```


## Description

Likelihood Ratio Tests for fitted cdfqr Objects.

## Usage

\#\# S3 method for class 'cdfqr'
anova(object, ..., test = "LRT")

## Arguments

object The fitted cdfqr model.
.. One or more cdfqr model objects for model comparison.
test The model comparison test, currently only 'LRT' is implemented.

## Examples

```
data(cdfqrExampleData)
fit_null <- cdfquantreg(crc99 ~ 1 | 1, 't2','t2', data = JurorData)
fit_mod1 <- cdfquantreg(crc99 ~ vert | conf1, 't2','t2', data = JurorData)
anova(fit_null, fit_mod1)
```

    AnxStrData Stress-Anxiety data
    
## Description

A data from a study that investigates the relationship between stress and anxiety.

## Usage

AnxStrData

## Format

A data frame with 166 rows and 2 variables:
Anxiety Scores on Anxiety subscale
Stress Scores on Stress subscale

## Source

https://pubmed.ncbi.nlm.nih.gov/16594767/
bugsLikelihood Likelihood Functions for Generating OpenBUGS Model File

## Description

Likelihood functions for generating OpenBUGS model file.

## Usage

bugsLikelihood(fd, sd)

## Arguments

fd A string that specifies the parent distribution.
sd A string that specifies the sub-family distribution.

## Value

A string to be written in the BUGS model file.

## Examples

```
    bugsLikelihood('t2','t2')
```


## Description

Generating OpenBUGS model file

## Usage

bugsModel(formula, fd, sd, random = NULL, modelname = "bugmodel", wd = getwd())

## Arguments

| formula | A formula object, with the DV on the left of an ~ operator, and predictors on the right. For the part on the right of ' $\sim$ ', the specification of submodels can be separated by ' 1 '. So $\mathrm{y} \sim \mathrm{X} 1 \mid \mathrm{X} 2$ means the DV is $\mathrm{y}, \mathrm{X} 1$ is the term in the mean submodel, and X 2 is the term in the dispersion submodel. |
| :---: | :---: |
| fd | A string that specifies the parent distribution (see cdfqrFamily). |
| sd | A string that specifies the sub-family distribution. |
| random | Character or vector of characters that indicates the random effect factors. |
| modelname | The name of the model file; optional. |
| wd | The working directory in which OpenBUGS will work (i.e., generate the model files and chain information). |

## Value

A model '.txt' file is generated in the specified working directory. The function also returns a list of values:
init1,init2 Default initial values for MCMC two chain procedure.
vars A list of variables that are included in the estimation.
nodes_sample a list of characters that specify the nodes to be monitored.

## Examples

```
    ## Not run:
    # Need write access in the working directory before executing the code.
    # No random component
    bugsModel(y ~ x1 | x2, 't2','t2', random = NULL)
    # Random component as subject ID
    bugsModel(y ~ x1 | x2, 't2','t2', random = 'ID')
    ## End(Not run)
```

    cdfft The Family of Finite-Tailed Distributions
    
## Description

Density function, distribution function, quantile function, and random generation of variates for a specified cdf-quantile distribution.

## Usage

cdfft(q, sigma, theta, fd, sd, mu = NULL, inner = TRUE, version)
pdfft(y, sigma, theta, fd, sd, mu = NULL, inner = TRUE, version)
qqft(p, sigma, theta, fd, sd, mu = NULL, inner = TRUE, version)
rqft(n, sigma, theta, fd, sd, mu = NULL, inner = TRUE, version)

## Arguments

q
sigma
theta
fd
sd
mu
inner
version
$y \quad$ vector of quantiles.
$p \quad$ vector of probabilities.
$\mathrm{n} \quad$ Number of random samples.

## Value

pdfft gives the density, rqft generates random variate, $q q f t$ gives the quantile function, and cdfft gives the cumulative density of specified distribution.

$$
\begin{array}{ll}
\text { cdfqr. control } & \begin{array}{l}
\text { Control Optimization Parameters for CDF-Quantile Probability Dis- } \\
\text { tributions }
\end{array}
\end{array}
$$

## Description

Control Optimization Parameters for CDF-Quantile Probability Distributions.

## Usage

cdfqr.control(method $=$ "BFGS", maxit $=5000$, trace $=$ FALSE)

## Arguments

$$
\begin{array}{ll}
\text { method } & \text { Characters string specifying the method argument passed to optim. } \\
\text { maxit } & \begin{array}{l}
\text { Integer specifying the maxit argument (maximal number of iterations) passed to } \\
\text { optim. }
\end{array} \\
\text { trace } & \begin{array}{l}
\text { Logical or integer controlling whether tracing information on the progress of the } \\
\text { optimization should be produced }
\end{array}
\end{array}
$$

## Value

A list with the arguments specified.

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2', 't2',
data = JurorData,control = cdfqr.control(trace = TRUE))
```

```
cdfqrFamily Overview of the family of distributions
```


## Description

The cdfquantreg family consists of the currently available distributions that can be used to fit quantile regression models via the cdfquantreg() function.

## Usage <br> cdfqrFamily(shape = "all")

## Arguments

shape $\quad$ To show all distributions or the set of distribution for a specific type of shape. Can be BM, TM, LL or FT for Bimodal, Trimodal, Logit-logistic or Finite-tailed shapes, respectively.

## Details

The cdfquantreg package includes a two-parameter family of distributions for modeling random variables on the $(0,1)$ interval by applying the cumulative distribution function (cdf) of one "parent" distribution to the quantile function of another.
The naming of these distributions is "parent - child" or " $\mathrm{fd}-\mathrm{sd}$ ", where " fd " is the parent distribution, and "sd" is the child distribution.
The distributions have four characteristic shapes: Logit-logistic, bimodal, trimodal, and finitetailed. Here is the list of currently available distributions.

## Bimodal Shape Distributions

Distribution
Burr VII-ArcSinh
Burr VII-Cauchy
Burr VII-T2
Burr VIII-ArcSinh
Burr VIII-Cauchy
Burr VIII-T2
Logit-ArcSinh
Logit-Cauchy
Logit-T2
T2-ArcSinh
T2-Cauchy
R input
fd = "burr7", sd = "arcsinh"
fd = "burr7", sd = "cauchy"
fd = "burr7", sd = "t2"
fd = "burr8", sd = "arcsinh"
fd = "burr8", sd = "cauchy"
fd = "burr8", sd = "t2"
fd = "logit", sd = "arcsinh"
fd = "logit", sd = "cauchy"
fd = "logit", sd = "t2"
fd = "t2", sd = "arcsinh"
fd = "t2", sd = "cauchy"

| Alternative Input | Shape |
| :--- | :---: |
| family = "burr7-arcsinh" | Bimodal |
| family = "burr7-cauchy" | Bimodal |
| family = "burr7-t2" | Bimodal |
| family = "burr8-arcsinh" | Bimodal |
| family = "burr8-cauchy" | Bimodal |
| family = "burr8-t2" | Bimodal |
| family = "logit-arcsinh" | Bimodal |
| family = "logit-cauchy" | Bimodal |
| family = "logit-t2" | Bimodal |
| family $=$ "t2-arcsinh" | Bimodal |
| family $=$ "t2-cauchy" | Bimodal |

## Trimodal Shape Distributions

| Distribution | R input | Alternative Input | Shape |
| :---: | :---: | :---: | :---: |
| ArcSinh-Burr VII | $\mathrm{fd}=$ "arcsinh", sd = "burr7" | family = "arcsinh-burr7" | Trimodal |
| ArcSinh-Burr VIII | $\mathrm{fd}=$ "arcsinh", sd = "burr8" | family = "arcsinh-burr8" | Trimodal |
| ArcSinh-Logistic | fd = "arcsinh", sd = "logistic" | family = "arcsinh-logistic" | Trimodal |
| ArcSinh-T2 | fd = "arcsinh", sd = "t2" | family = "arcsinh-t2" | Trimodal |
| Cauchit-Burr VII | fd = "cauchit", sd = "burr7" | family = "cauchit-burr7" | Trimodal |
| Cauchit-Burr VIII | $\mathrm{fd}=$ "cauchit", sd = "burr8" | family = "cauchit-burr8" | Trimodal |
| Cauchit-Logistic | fd = "cauchit", sd= "logistic" | family = "cauchit-logistic" | Trimodal |
| Cauchit-T2 | fd = "cauchit", sd= "t2" | family = "cauchit-t2" | Trimodal |
| T2-Burr VII | fd = "t2", sd = "burr7" | family = "t2-burr7" | Trimodal |
| T2-Burr VIII | $\mathrm{fd}=$ "t2", sd = "burr8" | family = "t2-burr8" | Trimodal |
| T2-Logistic | fd = "t2", sd= "logistic" | family = "t2-logistic" | Trimodal |

## Logit-logistic Shape Distributions

## Distribution

Burr VII-Burr VII
Burr VII-Burr VIII
Burr VII-Logistic
Burr VIII-Burr VII
Burr VIII-Burr VIII
Burr VIII-Logistic
Logit-Burr VII
Logit-Burr VIII
Logit-Logistic

## R input

fd = "burr7", sd = "burr7"
fd = "burr7", sd = "burr8"
fd = "burr7", sd = "logistic"
fd = "burr8", sd = "burr7"
fd = "burr8", sd = "burr8"
fd = "burr8", sd = "logistic"
fd = "logit", sd= "burr7"
fd = "logit", sd = "burr8"
fd = "logit", sd="logistic"

## Alternative Input

family = "burr7-burr7"
family = "burr7-burr8"
family = "burr7-logistic"
family = "burr8-burr7"
family = "burr8-burr8"
family = "burr8-logistic"
family = "logit-burr7"
family = "logit-burr8"
family = "logit-logistic"

## Shape

Logit-logistic Logit-logistic Logit-logistic Logit-logistic Logit-logistic Bimodal
Logit-logistic
Logit-logistic
Logit-logistic

## Finite-tailed Shape Distributions

| Distribution | R input | Alternative Input | Shape |
| :---: | :--- | :--- | :--- |
| ArcSinh-ArcSinh | $\mathrm{fd}=$ "arcsinh", $s d=" \operatorname{arcsinh"~}$ | family = "arcsinh-arcsinh" | Finite-tailed |


| ArcSinh-Cauchy | $\mathrm{fd}=$ "arcsinh", sd="cauchy" | family $=$ "arcsinh-cauchy" | Finite-tailed |
| :--- | :--- | :--- | :--- |
| Cauchit-ArcSinh | $\mathrm{fd}=$ "cauchit", sd="arcsinh" | family $=$ "cauchit-arcsinh" | Finite-tailed |
| Cauchit-Cauchy | $\mathrm{fd}=$ "cauchit", sd="cauchy" | family = "cauchit-cauchy" | Finite-tailed |
| T2-T2 | $\mathrm{fd}=$ "t2", sd="t2" | family $=" t 2-t 2 "$ | Finite-tailed |

## Kumaraswamy Distribution

| Distribution | R input | Alternative Input | Shape |
| :--- | :--- | :--- | :--- |
| Kumaraswamy | $f d=" ", s d=" "$ | family $="-"$ |  |

## Value

A list of distributions that are available in the current version of package.

## Examples

cdfarFamily()

```
cdfquantreg CDF-Quantile Probability Distributions
```


## Description

cdfquantreg is the main function to fit a cdf quantile regression with a variety of distributions.

## Usage

```
cdfquantreg(
        formula,
        fd = NULL,
        sd = NULL,
        data,
        family = NULL,
        start = NULL,
        control = cdfqr.control(...),
    )
```


## Arguments

formula A formula object, with the dependent variable (DV) on the left of an ~ operator, and predictors on the right. For the part on the right of ' $\sim$ ', the specification of the location and dispersion submodels can be separated by 'l'. So y ~ X1 | X2 specifies that the DV is $\mathrm{y}, \mathrm{X} 1$ is the predictor in the location submodel, and X 2 is the predictor in the dispersion submodel.

| fd | A string that specifies the parent distribution. |
| :--- | :--- |
| sd | A string that specifies the child distribution. |
| data | The data in a data.frame format |
| family | If 'fd' and 'sd' are not provided, the name of a member of the family of distri- <br> butions can be provided (See cdfarFamily for details of family functions) |
| start | The starting values for model fitting. If not provided, default values will be used. <br> control |
| Control optimization parameters (See cdfqr. control)) |  |
| $\ldots$ | Currently ignored. |

## Details

The cdfquantreg function fits a quantile regression model with a distributions from the cdf-quantile family selected by the user (Smithson and Shou, 2015). The model is specified in a two-part formula, one part containing the predictors of the location parameter, and the second part containing the predictors of the dispersion parameter. The models are fitted in two stages, the first of which uses the Nelder-Mead algorithm and the second of which takes the estimates from the first stage and applies the BFGS algorithm to refine the estimates.

## Value

An object of class cdfquantreg will be returned. Generic functions such as summary,print (e.g., print.cdfqr) and coef can be used to extract output (see summary.cdfqr for more details about the generic functions that can be used). Class of object is a list with the following output:
coefficients A named vector of coefficients.
residuals Raw residuals, the difference between the fitted values and the data.
fitted The fitted values, including full model fitted values, fitted values for the mean component, and fitted values for the dispersion component.
rmse The model root mean squared errors
rmseLogit The root mean squared errors between the logit of the fitted values, and the logit of the response values.
vcov The variance-covariance matrix of the coefficient estimates.
AIC, BIC Akaike's Information Criterion and Bayesian Information Criterion.
deviance The deviance for the model.

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, fd ='t2',sd ='t2', data = JurorData)
summary(fit)
```


## Description

cdfquantregC is the a function to fit a censored cdf quantile regression with a variety of distributions.

## Usage

cdfquantregC(
formula,
$\mathrm{fd}=$ NULL,
sd = NULL,
data,
family = NULL,
censor = "DB",
c1 = NULL,
c2 = NULL,
start = NULL,
control $=$ cdfqr. control(...),
)

## Arguments

| formula | A formula object, with the dependent variable (DV) on the left of an ~ operator, and predictors on the right. For the part on the right of ' $\sim$ ', the specification of the location and dispersion submodels can be separated by ' 1 '. So y $\sim X 1 \mid X 2$ specifies that the DV is $\mathrm{y}, \mathrm{X} 1$ is the predictor in the location submodel, and X 2 is the predictor in the dispersion submodel. |
| :---: | :---: |
| fd | A string that specifies the parent distribution. |
| sd | A string that specifies the child distribution. |
| data | The data in a data.frame format |
| family | If 'fd' and 'sd' are not provided, the name of a member of the family of distributions can be provided (See cdfqrFamily for details of family functions) |
| censor | A string variable to indicate how many censored point is used- only left censored `LC', or only right-hand censored `RC', or both sides `DB'. |
| c1 | The left censored value, if NULL, the minimum value in the data will be used |
| c2 | The right censored value, if NULL, the maximum value in the data will be used |
| start | The starting values for model fitting. If not provided, default values will be used. |
| control | Control optimization parameters (See cdfqr.control)) |
|  | Currently ignored. |

## Details

The cdfquantreg function fits a quantile regression model with a distributions from the cdf-quantile family selected by the user (Smithson and Shou, 2015). The model is specified in a two-part formula, one part containing the predictors of the location parameter, and the second part containing the predictors of the dispersion parameter. The models are fitted in two stages, the first of which uses the Nelder-Mead algorithm and the second of which takes the estimates from the first stage and applies the BFGS algorithm to refine the estimates.

## Value

An object of class cdfquantreg will be returned. Generic functions such as summary,print (e.g., print.cdfqr) and coef can be used to extract output (see summary.cdfqr for more details about the generic functions that can be used). Class of object is a list with the following output:
coefficients A named vector of coefficients.
residuals Raw residuals, the difference between the fitted values and the data.
fitted The fitted values, including full model fitted values, fitted values for the mean component, and fitted values for the dispersion component.
rmse The model root mean squared errors
rmseLogit The root mean squared errors between the logit of the fitted values, and the logit of the response values.
vcov The variance-covariance matrix of the coefficient estimates.
AIC, BIC Akaike's Information Criterion and Bayesian Information Criterion.
deviance The deviance for the model.

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantregC(crc99 ~ vert | confl, c1 = 0.001, c2= 0.999,
fd ='t2',sd ='t2', data = JurorData)
```

summary(fit)

## Description

cdfquantregFT is a function to fit a cdf quantile regression with a variety of finite tailed distributions. It can account for data that has boundary values.

```
Usage
    cdfquantregFT(
        formula,
        fd \(=\) NULL,
        sd = NULL,
        mu.fo = NULL,
        inner = FALSE,
        version = "V",
        data,
        family = NULL,
        start = NULL,
        ssn = 20,
        control \(=\) cdfqr.control(...),
    ...
)
```


## Arguments

| formula | A formula object, with the dependent variable (DV) on the left of an $\sim$ operator, and predictors on the right. For the part on the right of ' $\sim$ ', the specification of the dispersion (sigma; first) and skewness (theta; second) submodels can be separated by 'l'. So $y \sim X 1 \mid X 2$ specifies that the $D V$ is $y, X 1$ is the predictor in the dispersion submodel, and X 2 is the predictor in the skewness submodel. |
| :---: | :---: |
| fd | A string that specifies the parent distribution. At the moment, only "arcsinh", "cauchit" and "t2" can be used. See details. |
| sd | A string that specifies the child distribution. At the moment, only "arcsinh", "cauchy" and "t2" can be used. See details. |
| mu.fo | A formula object to indicate the predictors for the location submodel if the 3parameter distribution is used, only input as ~ predictors |
| inner | A logic value that indicates if the inner (inner $=$ TRUE) case or outer (inner = FALSE) will be used. Currently inner case can only be used for 2-parameter distributions. |
| version | A string indicates that which version will be used. " V " is the tilt transformation while "W" indicates the Jones Pewsey transformation. |
| data | The data in a data.frame format |
| family | If 'fd' and 'sd' are not provided, the name of a member of the family of distributions can be provided (see below) for details of family functions) |
| start | The starting values for model fitting. If not provided, default values will be used. |
| ssn | The number of searches on optimal starting values to be performed. If model does not converge, can increase this number. |
| control | Control optimization parameters (See cdfqr.control)) |
|  | Currently ignored. |

## Details

The cdfquantregFT function fits a quantile regression model with a distributions from the cdfquantile finite tailed distributions. Here is the list of currently available distributions.

## Bimodal Shape Distributions

| Distribution | $\mathbf{R}$ input | Alternative Input | Available Version |
| :---: | :---: | :---: | :---: |
| ArcSinh-ArcSinh | fd = "arcsinh", sd = "arcsinh" | family = "arcsinh-arcsinh" | "V", "W" |
| ArcSinh-Cauchy | fd = "arcsinh", sd = "cauchy" | family = "arcsinh-cauchy" | "V", "W" |
| Cauchit-ArcSinh | fd = "cauchit", sd = "arcsinh" | family = "cauchit-arcsinh" | "V", "W" |
| Cauchit-Cauchy | fd = "cauchit", sd = "cauchy" | family = "cauchit-cauchy" | "V", "W" |
| T2-T2 | fd = "t2", sd = "t2" | family = "t2-cauchy" | "V", "W" |

## Value

An object of class cdfqrFT will be returned. Generic functions such as summary, print and coef can be used to extract output (see summary.cdfqr for more details about the generic functions that can be used). Class of object is a list with the following output:
coefficients A named vector of coefficients.
residuals Raw residuals, the difference between the fitted values and the data.
fitted The fitted values, including full model fitted values, fitted values for the mean component, and fitted values for the dispersion component.
rmse The model root mean squared errors
rmseLogit The root mean squared errors between the logit of the fitted values, and the logit of the response values.
vcov The variance-covariance matrix of the coefficient estimates.
AIC, BIC Akaike's Information Criterion and Bayesian Information Criterion.
deviance The deviance for the model.

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantregFT(pnurse ~ Ambulance |Ambulance ,
    fd = "arcsinh", sd = "arcsinh", inner = FALSE, version = "V", data = yoon)
summary(fit)
```

cdfquantregH Zero/One inflated CDF-Quantile Probability Distributions

## Description

cdfquantregH is the a function to fit a Zero/One inflated CDF-Quantile regression with a variety of distributions .

## Usage

cdfquantregH(
formula,
zero. fo $=\sim 1$,
one.fo $=\sim 1$,
fd $=$ NULL,
sd = NULL,
data,
family = NULL,
type = "ZI",
start = NULL,
control $=$ cdfqr.control(...),
)

## Arguments

formula A formula object, with the dependent variable (DV) on the left of an ~ operator, and predictors on the right. For the part on the right of ' $\sim$ ', the specification of the location and dispersion submodels can be separated by 'l'. So y $\sim X 1 \mid X 2$ specifies that the DV is $\mathrm{y}, \mathrm{X} 1$ is the predictor in the location submodel, and X 2 is the predictor in the dispersion submodel.
zero.fo A formula object to indicate the predictors for the zero component, only input as ~predictors
one.fo A formula object to indicate the predictors for the one component, only input as ~ predictors
$\mathrm{fd} \quad$ A string that specifies the parent distribution.
sd A string that specifies the child distribution.
data The data in a data.frame format
family If 'fd' and 'sd' are not provided, the name of a member of the family of distributions can be provided (See cdfqrFamily for details of family functions)
type A string variable to indicate whether the model is zero-inflated `ZI`, or oneinflated `OI', or zero-one inflated `ZO'.
start The starting values for model fitting. If not provided, default values will be used.
control Control optimization parameters (See cdfqr.control))
... Currently ignored.

## Details

The cdfquantreg function fits a quantile regression model with a distributions from the cdf-quantile family selected by the user (Smithson and Shou, 2015). The model is specified in a two-part formula, one part containing the predictors of the location parameter, and the second part containing the predictors of the dispersion parameter. The models are fitted in two stages, the first of which uses the Nelder-Mead algorithm and the second of which takes the estimates from the first stage and applies the BFGS algorithm to refine the estimates.

## Value

An object of class cdfqrH will be returned. Generic functions such as summary,print (e.g., print.cdfqr) and coef can be used to extract output (see summary.cdfqr for more details about the generic functions that can be used). Class of object is a list with the following output:
coefficients A named vector of coefficients.
residuals Raw residuals, the difference between the fitted values and the data.
fitted The fitted values, including full model fitted values, fitted values for the mean component, and fitted values for the dispersion component.
vcov The variance-covariance matrix of the coefficient estimates.
AIC, BIC Akaike's Information Criterion and Bayesian Information Criterion.

## Examples

```
data(cdfqrExampleData)
# For one-inflated model
ipcc_high <- subset(IPCC, mid == 1 & high == 1 & prob!=0)
fit <- cdfquantregH(prob ~ valence | valence,one.fo = ~valence,
    fd ='t2',sd ='t2', type = "OI", data = ipcc_high)
summary(fit)
# For zero-inflated model
ipcc_low <- subset(IPCC, mid == 0 & high == 0 & prob!=1)
fit <- cdfquantregH(prob ~ valence | valence, zero.fo = ~valence,
        fd ='t2',sd ='t2', type = "ZI", data = ipcc_low)
# For zero &one-inflated model
ipcc_mid <- subset(IPCC, mid == 1 & high == 0)
fit <- cdfquantregH(prob ~ valence | valence, zero.fo = ~valence,
    one.fo = ~valence,
    fd ='t2',sd ='t2', type = "zO", data = ipcc_mid)
```


## Description

Density function, distribution function, quantile function, and random generation of variates for a specified cdf-quantile distribution.

## Usage

dq(x, mu, sigma, fd, sd)
rq(n, mu, sigma, fd, sd)
$q q(p$, mu, sigma, fd, sd)
pq(q, mu, sigma, fd, sd)

## Arguments

x
mu
sigma
fd A string that specifies the parent distribution.
sd A string that specifies the sub-family distribution.
$\mathrm{n} \quad$ Number of random samples.
$p \quad$ vector of probabilities.
$q \quad$ vector of quantiles.

## Value

dq gives the density, rq generates random variates, qq gives the quantile function, and pq gives the cumulative density of specified distribution.

## Examples

```
    \(x<-r q(5, m u=0.5\), sigma \(=1, ~ ' t 2 ', ' t 2 ') ; x\)
    dq(x, mu = 0.5, sigma = 1, 't2','t2')
    qtil <- pq(x, mu = 0.5, sigma \(=1\), 't2','t2');qtil
    qq(qtil , mu = 0.5, sigma \(=1\), 't2','t2')
```

    ExtEvent
        Extinction Study data-set
    
## Description

Probability of Human Extinction Study

## Usage

ExtEvent

## Format

A data frame with 1170 rows and 11 variables:
ID Subject ID
gend Gender of subjects, ' 0 'is male, ' 1 'is female
nation The nation of the participants come from
UK effect coding for nation
IND effect coding for nation
political political orientation of subjects
format The format of probability elicitation
order the order of probability judgement task.
SECS_6 Social conservativsm question on attitude toward gun ownership.
EQ1_P Probability estimates for general threats.
EQ3_P Probability estimates for the greatest threat.

## Source

https://www.michaelsmithson.online/
influence.cdfqr Influence Diagnosis For Fitted Cdfqr Object

## Description

Influence Diagnosis (dfbetas) For Fitted Cdfqr Object

## Usage

```
## S3 method for class 'cdfqr'
    influence(
        model,
        method = "dfbeta",
        type = c("full", "location", "dispersion", "skew", "zero", "one"),
        what = "full",
        plot = FALSE,
        id = FALSE,
    )
    ## S3 method for class 'cdfqr'
    dfbeta(
        model,
        type = c("full", "location", "dispersion", "skew", "zero", "one"),
        what = "full",
```

```
)
## S3 method for class 'cdfqr'
dfbetas(
    model,
        type = c("full", "location", "dispersion", "skew", "zero", "one"),
        what = "full",
    ..
)
```


## Arguments

| model | A cdfqr model object |
| :--- | :--- |
| method | Currently only 'dfbeta' method is available. |
| type | A string that indicates whether the results for all parameters are to be returned, <br> or only the submodel's parameters returned. |
| what | for influence statistics based on coefficient values, indicate the predictor vari- <br> ables that needs to be tested. |
| plot | if plot is needed. <br> id |
| $\ldots$ | for plot only, if TRUE, the case ids will be displayed in the plot. |
| $\ldots$ | Pass onto other functions or currently ignored |

## Value

A matrix, each row of which contains the estimated influence on parameters when that row's observation is removed from the sample.

## See Also

lm.influence, influence.measures

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2', 't2', data = JurorData)
#It takes some time especially the data is large.
influcne <- influence(fit)
plot(influcne[,2])
## Not run:
# Same as influence(fit)
dfbetval <- dfbetas(fit)
## End(Not run)
```

| IPCC | IPCC data-set |
| :--- | :--- |

## Description

The IPCC data-set comprises the lower, best, and upper estimates for the phrases "likely" and "unlikely" in six IPCC report sentences.

## Usage

IPCC

## Format

A data frame with 4014 rows and 8 variables:
subj Subject ID number
treat Experimental conditions
valence Valence of the sentences
prob raw probability estimates
probm Linear transformed prob into $(0,1)$ interval
mid Distinguish lower, best and upper estiamtes
high Distinguish lower, best and upper estiamtes
Question IPCC question number

## Source

https://pubmed.ncbi.nlm.nih.gov/19207697/

## Description

The IPCC-AUS data-set comprises the best estimates for the phrases in IPCC report sentences.

## Usage

IPCCAUS

## Format

A data frame with 4014 rows and 8 variables:

## ID Subject ID

gender Gender of subjects, ' 0 'is male, ' 1 'is female
age age of subjects
cfprob personal probability.
bestprob nominated probability.

## Source

https://pubmed.ncbi.nlm.nih.gov/19207697/

IPCC_Wide IPCC data-set - Wide format

## Description

The IPCC-wide data-set comprises the best estimates for the phrases "likely" and "unlikely" in six IPCC report sentences.

## Usage

IPCC_Wide

## Format

A data frame with 4014 rows and 8 variables:
Q4 Each column indicates the estimates for one sentence.
Q5 Each column indicates the estimates for one sentence.
Q6 Each column indicates the estimates for one sentence.
Q8 Each column indicates the estimates for one sentence.
Q9 Each column indicates the estimates for one sentence.
Q10 Each column indicates the estimates for one sentence.

## Source

https://pubmed.ncbi.nlm.nih.gov/19207697/

```
    JurorData Juror data
```


## Description

Juror Judgment Study.

## Usage

JurorData

## Format

A data frame with 104 rows and 3 variables:
crc99 The ratings of confidence levels with rescaling into the $(0,1)$ interval to avoide 1 and 0 values.
vert was the dummy variable for coding the conditions of verdict types, whereas
confl was the dummy variable for coding the conflict conditions

## Source

doi:10.1375/pplt.2004.11.1.154
plot.cdfqr
Plot Fitted Values/Residuals of A Cdfqr Object or Distribution

## Description

Plot Fitted Values/Residuals of A cdfqr Object or Distribution

```
Usage
    ## S3 method for class 'cdfqr'
    plot(
        x,
        mu = NULL,
        sigma = NULL,
        theta = NULL,
        fd = NULL,
        sd = NULL,
        n = 10000,
        inner = TRUE,
        version = "V",
        type = c("fitted"),
    )
```


## Arguments

X
mu
sigma

## theta

fd
sd
n
inner
version
type
...

If the plot is based on the fitted values, provide a fitted cdfqr object, alternatively, mu and sigma, and the distribution can be specified.
Location parameter value
Sigma parameter value
Skew parameter value
A string that specifies the parent distribution.
A string that specifies the sub-family distribution.
The number of random variates to be generated for user specified plot.
If finite-tailed distribution is used: a logic value that indicates if the inner (inner $=$ TRUE) case or outer (inner $=$ FALSE) will be used. Currently inner case can only be used for 2-parameter distributions.

Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2','t2', data = JurorData)
plot(fit)
```

    predict.cdfqr Methods for Cdfqr Objects
    
## Description

Methods for obtaining the fitted/predicted values for a fitted cdfqr object.

## Usage

```
## S3 method for class 'cdfqr'
predict(
        object,
        newdata = NULL,
        type = c("full", "mu", "sigma", "theta", "one", "zero"),
        quant = 0.5,
    )
```

```
## S3 method for class 'cdfqr'
fitted(
    object,
    type = c("full", "mu", "sigma", "theta", "one", "zero"),
    plot = FALSE,
)
```


## Arguments

| object | A cdfqr model fit object |
| :--- | :--- |
| newdata | Optional. A data frame in which to look for variables with which to predict. If <br> not provided, the fitted values are returned |
| type | A character that indicates whether the full model prediction/fitted values are <br> needed, or values for the 'mu' and 'sigma' submodel only. |
| quant | A number or a numeric vector (must be in $(0,1))$ to specify the quantile(s) of the <br> predicted value (when 'newdata' is provided, and predicted values for responses <br> are required). The default is to use median to predict response values. |
| $\ldots$ | currently ignored <br> plot |

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2','t2', data = JurorData)
plot(predict(fit))
plot(predict(fit))
```

qrBoot Bootstrapping for cdf quantile regression

## Description

qrBoot provides a simple bootstrapping method for estimating the parameters of a cdf quantile regression model.

## Usage

qrBoot(object, rn, f = coef, $\mathrm{R}=500$, ci $=0.95$ )

## Arguments

object The fitted cdfqr model object
rn The sample size of bootstrap samples
$f \quad$ A function whose one argument is the name of a cdfqr object that will be applied to the updated cdfqr object to compute the statistics of interest. The default is coef.

R
Number of bootstrap samples.
ci
The confidence interval level to obtain the bootstrap confidence intervals

## Value

A matrix that includes the original statistics, bootstrap means, and bootstrap confidence intervals

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2', 't2', data = JurorData)
qrBoot(fit, rn = 50, R = 50)
```

qrGrad

Give the Gradient Function for CDF-Quantile Distribution Models

## Description

Give the Gradient Function for CDF-Quantile Distribution models

## Usage

$\operatorname{qrGrad}(f d, s d)$

## Arguments

fd A string that specifies the parent distribution.
sd A string that specifies the sub-family distribution.

## Value

grad The gradient function of parameter estimates, given a specified cdf-quantile distribution

## Examples

```
    qrGrad('t2','t2')
```


## Description

Function to give the (negative) log likelihood for fitting cdfquantile distributions.

## Usage

qrLogLik(y, mu, sigma, fd, sd, total = TRUE)

## Arguments

$y \quad$ the vector to be evaluated.
mu mean of the distribution.
sigma sigma of the distribution.
$\mathrm{fd} \quad$ A string that specifies the parent distribution.
sd A string that specifies the sub-family distribution.
total whether the sum of logliklihood is calculated

## Value

The negative log likelihood for fitting the data with a cdfquantile distribution.

## Examples

```
y <- rbeta(20, 0.5, 0.5)
qrLogLik(y, mu = 0.5, sigma = 1, 't2','t2')
```

qrPwlm Probability Weighted L-moment Skewness and Kurtosis

## Description

Calculate the skew and kurtosis statistics based on probability weighted moments, via simulation method.

## Usage

$\operatorname{qrPwlm}(x, \mathrm{n}=$ NULL, $m u=$ NULL, sigma $=$ NULL, fd $=$ NULL, $s d=$ NULL)

## Arguments

$x \quad$ The vector of values for the calculation of Skewness and Kurtosis.
$\mathrm{n} \quad$ The number of samples drawn in the simulation. The higher this value, the greater accuracy.
mu vector of means.
sigma vector of standard deviations.
fd A string that specifies the parent distribution.
sd A string that specifies the sub-family distribution.

## Details

This function computes the L-moment measures of skew and kurtosis, which may be computed via linear combinations of probability-weighted moments (Greenwood, Landwehr, Matalas and Wallis, 1979).

## Value

The tau3(skew) and tau4(kurtosis) values of the L-moment.

## References

Greenwood, J. A., Landwehr, J. M., Matalas, N. C., \& Wallis, J. R. (1979). Probability weighted moments: definition and relation to parameters of several distributions expressable in inverse form. Water Resources Research, 15(5), 1049-1054.

## Examples

qrPwlm(n = 1000, mu = 0.5, sigma = 1, fd = 't2', sd = 't2')

```
qrStart
```

Starting Value Generation for CDF quantile Regressions

## Description

qrStart is the function for generating starting values for a cdf-quantile GLM null model.

## Usage

qrStart(ydata, $f d=$ NULL, $s d=$ NULL, skew $=$ FALSE)

## Arguments

ydata The variable to be modeled
fd A string that specifies the parent distribution.
sd A string that specifies the sub-family distribution.
skew If ture, the starting values will be generated for the finited tailed distribution case.

## Details

The start values for the location parameter in a null model are the median of the empirical distribution, and a starting value for the dispersion parameter based on a specific quantile of the empirical distribution, specified according to the theoretical distribution on which the model is based. The start values for all new predictor coefficients in both the location and dispersion submodels are assigned the value 0.1.

## Value

A vector that consists initial values for mu and sigma.

## Examples

```
x <- rbeta(100, 1, 2)
qrStart(x, fd='t2', sd='t2')
#[1] -0.5938286 1.3996999
```

```
residuals.cdfqr Register method for cdfqr object functions
```


## Description

Register method for cdfqr object functions.

## Usage

\#\# S3 method for class 'cdfqr'
residuals(object, type = c("raw", "pearson", "deviance"), ...)

## Arguments

object The cdfqr model project
type The type of residuals to be extracted: 'raw', 'pearson','std.pearson', or 'deviance',
... currently ignored

## Value

residuals of a specified type.

## Examples

data(cdfarExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2','t2', data = JurorData)
residuals(fit, "pearson")
scaleTR
Transform Values into $(0,1)$ Interval

## Description

scaleTR is function that rescales values of a variable into the $(0,1)$ interval.

## Usage

scaleTR(y, high $=$ NULL, low $=$ NULL, data $=$ NULL, $N=$ NULL, scale = 0.5)

## Arguments

$y \quad$ A numeric vector, or a variable in a dataframe.
high The highest possible value of that variable. The value should be equal or greater than the maximum value of $y$. If not supplied, the maximum value of $y$ will be used.
low The lowest possible value of that variable. The value should be equal or smaller than the minimum value of $y$. If not supplied, the minimum value of $y$ will be used.
data A dataframe that contains the variable y .
$N \quad$ A integer, normally is the sample size or the number of values. If not supplied, the length of $y$ will be used.
scale A compressing parameter that determines the extend to which the boundary values are going to be pushed away from the boundary. See details.

## Details

scaleTR used the method suggested by Smithson and Verkuilen (2006) and applies linear transformation to values into the open interval $(0,1)$. It first transform the values from their original scale by taking $y^{\prime}=(y-a) /(b-a)$, where a is the lowest possible value of that variable and b is the highest possible value of that variable. Next, it compresses the range to avoid zeros and ones by taking $y^{\prime \prime}=\left(y^{\prime}(N-1)+c\right) / N$, where N is the sample size and c is the compressing parameter. The smaller value $c$ is, the boundary values would be more approaching zeros and ones, and have greater impact on the estimation of the dispersion parameters in the cdf quantile model.

## See Also

cdfquantreg

## Examples

$y<-\operatorname{rnorm}(20,0,1)$
ynew <- scaleTR(y)
summary.cdfqr

```
summary.cdfqr
```

S3 Methods for getting output from fitted cdfqr Objects.

## Description

Give the S3 Methods for CDF-Quantile Distribution Models

## Usage

```
## S3 method for class 'cdfqr'
summary(object, ...)
    ## S3 method for class 'cdfqr'
    print(x, digits = max(3, getOption("digits") - 3), ...)
    ## S3 method for class 'cdfqr'
    coef(object, type = "full", ...)
    ## S3 method for class 'cdfqr'
    vcov(object, type = "full", ...)
    ## S3 method for class 'cdfqr'
    update(object, formula., zero.fo., one.fo., mu.fo., ..., evaluate = TRUE)
    ## S3 method for class 'cdfqr'
    confint(object, parm, level = 0.95, submodel = "full", ...)
    ## S3 method for class 'cdfqr'
    formula(x, ...)
    ## S3 method for class 'cdfqr'
    nobs(object, ...)
    ## S3 method for class 'cdfqr'
    deviance(object, ...)
    ## S3 method for class 'cdfqrH'
    logLik(object, ...)
    ## S3 method for class 'cdfqrH'
    confint(
        object,
        parm,
        level = 0.95,
        type = c("full", "mean", "sigma", "zero", "one"),
    )
```

```
## S3 method for class 'cdfqrFT'
confint(object, parm, level = 0.95, submodel = "full", ...)
```


## Arguments

|  | Pass onto other functions or currently ignored |
| :---: | :---: |
| $x$, object | The fitted cdfqr model. |
| digits | Number of digits to be retained in printed output. |
| type, submodel | The parts of coefficients or variance-covariance matrix to be extracted.Can be "full", "mean",or "sigma". |
| zero.fo., one.fo., mu.fo., |  |
|  | Changes to the formulas for zero/one component for hurdle models, and for location submodel for finite-tailed models. |
| evaluate | If true evaluate the new updated model else return the call for the new model. |
| parm | a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered. |
| level | the confidence level required. |

## Examples

```
data(cdfqrExampleData)
fit <- cdfquantreg(crc99 ~ vert | confl, 't2','t2', data = JurorData)
summary(fit)
print(fit)
logLik(fit)
coef(fit)
deviance(fit)
vcov(fit)
confint(fit)
#Update the model
fit2 <- update(fit, crc99 ~ vert*confl | confl)
summary(fit2)
```


## Description

Data from Modeling Proportion of Patient Time in Emergency Ward Stages

## Usage

yoon

## Format

A data frame with 1170 rows and 11 variables:
id case identification
Day day of the week ( $0=$ Sunday)
Ambulance $0=$ walk-in; $1=$ ambulance-arrival
Triage triage level
Triage1 $1=$ triage level 1
Triage2 1 = triage level 2
Triage3 $1=$ triage level 3
Triage4 $1=$ triage level 4
Triage5 $1=$ triage level 5
Lab 1 = laboratory test(s) conducted
Xray 1 = x-ray conducted
Other $1=$ other intervention
LOS length of stay in minutes
LOSh length of stay in hours
preg proportion of time in registration stage
ptriage proportion of time in triage stage
pnurse proportion of time in nursing care stage
pphysician proportion of time in consultation with physician(s)
pdecis proportion of time in decisional stage
pregptriage preg + ptriage
pphysdecis pphysician + pdecis
prnurse pnurse/(pnurse + pregptriage)
prphysdec pphysdecis /(pphysdecis + pregptriage)

## Source

doi:10.1017/S1481803500006539

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